

## Article

# Lattice Design of an Intermediate-Energy Electron Storage Ring Dedicated to Materials Research

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**Abstract:** Storage ring X-ray light sources, which hold the great promises of high flux, high average brilliance, high stability, continuously adjustable spectra, and simultaneous multiple end-stations operations, have become indispensable tools for frontier research in diverse fields from materials science, condensed matter physics, chemistry, to life science, etc. Based on the double double-bend achromat (DDBA) lattice structure, an intermediate-energy electron storage ring with circumference of 288 m, emittance of 2.57 nm, is designed for dedicated materials research. Each cell of the storage ring consists of a 6.2 m-long straight section and a 1.86 m-short straight section, allowing more insertion devices to be accommodated in the entire ring. This lattice shows great nonlinear dynamic performances of large dynamic aperture and large local momentum aperture. Furthermore, the intra-beam scattering (IBS) effects under several circumstances, are also negligibly small.

**Keywords:** storage ring; lattice design; linear optics; nonlinear optics; intra-beam scattering; brilliance



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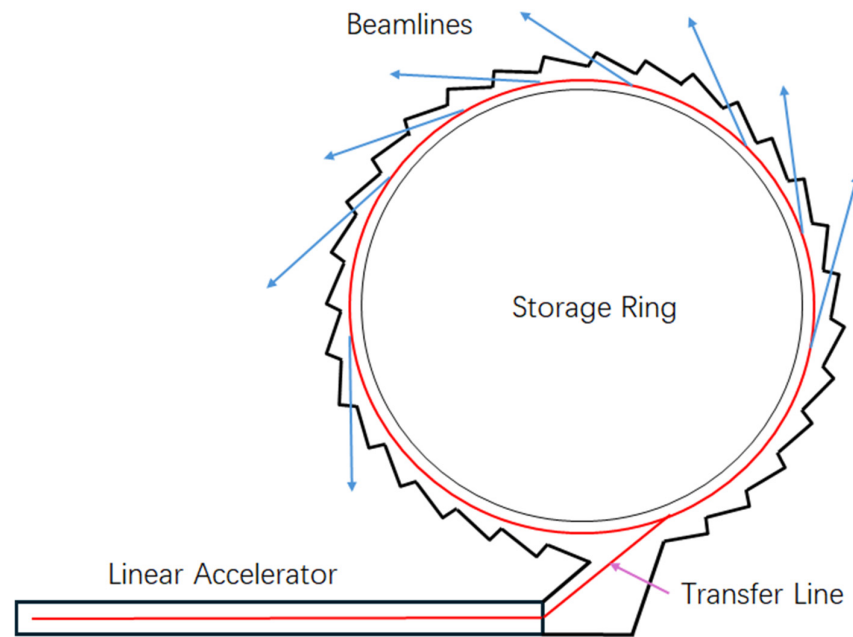
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## 1. Introduction

Light sources are powerful tools for the development of human civilization, and every advance in them has greatly enhanced people's ability to understand and control the unknown world, and given a strong impetus to the development of science and technology. X-ray light sources are indispensable cutting-edge instruments for observing the internal structure of objects, and for probing and understanding the microscopic structure and dynamic processes within matter at the molecular and atomic scales. The storage ring light source is one of the world's leading synchrotron radiation facilities today and is a cost-effective, highly reliable, and stable user facility. The storage ring light source provides high flux, high average brilliance X-ray with a broad, continuously tunable photon energy spectrum from infrared to hard X-ray, accommodates dozens of beamlines and experimental stations, and allows a wide range of experiments to be performed simultaneously at each station [1].

Figure 1 shows a schematic diagram of a typical storage ring light source, which consists of a full-energy injector, a beam transport line, and a storage ring. The storage ring light source has become an indispensable experimental tool in various fields of science and technology, such as applications in frontier research in physics, chemistry, materials science, environmental science, biology, and life science.



**Figure 1.** Schematic diagram of a storage ring light source.

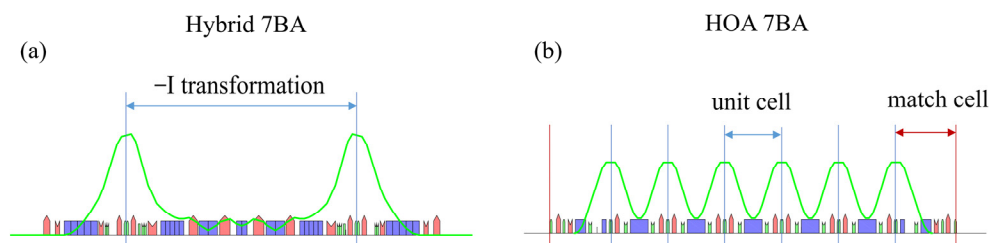
Brilliance is defined as the ratio of the photon spectral flux to the volume of the convolution between the electron beam and the photon beam in the two transverse dimensions. Brilliance is one of the most important performance parameters of a storage ring light source. The storage ring light source has gone through three generations of development and is currently under active development towards the fourth-generation light source, the diffraction-limited storage ring (DLSR), whose average brilliance is about 2–3 orders of magnitude higher than that of the third-generation storage ring light source [1,2]. The DLSR improves the brilliance of the storage ring light source mainly by reducing the emittance of the electron beam to approach or reach the diffraction limit of X-rays. The emittance of the electron beam can be evaluated using the following simple formula:

$$\varepsilon_{x0} = \frac{C_q \gamma^2}{J_x} F \theta^3, \quad (1)$$

where  $C_q = 3.83 \times 10^{-13}$  m,  $\gamma$  is the Lorentz factor,  $J_x$  is the horizontal damping partition number,  $\theta$  is the bending angle of each bending magnet, and  $F$  is a dimensionless numerical factor related to the lattice structure of the storage ring. Equation (1) assumes that all dipoles are of the same specification, i.e., have the same length and deflection radius. Given a fixed beam energy, the most effective method of reducing the emittance is to reduce the bending angle of each bending magnet, i.e., to increase the number of bending magnets in each cell, which is the basic idea of the multi-bend achromat (MBA) structure.

Currently, four DLSRs based on the MBA structure are in operation, namely MAX-IV [3,4], Sirius [5], ESRF-EBS [6,7], and APS-U [8]. In addition, many MBA storage rings are under commissioning, construction, or planning, including HEPS [9], PETRA-IV [10], SPring-8-II [11], Korea-4GSR [12], Diamond-II [13], SAPS [14], SSRL-X [15], SOLEIL II [16], SLS 2.0 [17], Elettra 2.0 [18], HALF [19], ALS-U [20], etc. Except for HEPS, Korea-4GSR, SAPS, SSRL-X, MAX IV, Sirius, and HALF, which are green-field light sources, all other light sources are upgraded from the old third-generation facilities to the DLSRs. The lattice structures of these facilities can be mainly divided into two categories: one is the hybrid MBA and the other is the higher-order achromat (HOA) MBA. The schematic diagram of the MBA lattice structures and dispersion function trends of hybrid MBA and HOA

MBA is shown in Figure 2. The hybrid MBA structure is characterized by two dispersion bumps, where the sextupole magnets for chromaticity correction are placed only within the dispersion bump, and the sextupole magnets satisfy the  $-I$  transformation between them, which means that the phase advance between the sextupole magnets is generally  $(3\pi, \pi)$  [21]. This can cancel out the nonlinear effects introduced by the sextupole magnets themselves, facilitating better nonlinear dynamic performance. The HOA MBA structure employs distributed sextupole magnets for chromaticity correction, where each unit cell contains chromaticity sextupole magnets, and each unit cell satisfies a certain phase advance to cancel out the nonlinear effects [22,23]. The HOA MBA has a very large number of magnets in one cell due to several  $(M-2)$  small repeating unit cells and two matching cells. When the HOA MBA structure is used in a high-energy storage ring light source, the length of one cell is much larger than that of one cell of the hybrid MBA, under the restriction of the same magnetic strength. The hybrid MBA structure uses a large number of combined dipole-quadrupole magnets and does not use distributed sextupole magnets, and the number of magnets in one unit is moderate. Therefore, the hybrid MBA structure is generally suitable for high-energy large rings, while the HOA MBA structure is more suitable for low-energy small rings.



**Figure 2.** Schematic diagram of the MBA lattice structure (assuming  $M = 7$ ,  $M$  represents the number of bending magnets in one cell) and dispersion function (green line) trend of (a) hybrid 7BA and (b) HOA 7BA. The blue rectangles in the figure represent the dipoles, the red polygons represent quadrupoles, and the green polygons represent sextupoles.

However, DLSRs are not the only direction of the storage ring light source the community is pursuing. We are also witnessing another emerging direction, pioneered by the NanoTerasu project [24], and followed by the SPS-II project [25], which aims at not the utmost brilliance but rather high stability, reliability, and flux with moderate emittance and more relaxed specifications to related instrumentations. In this paper, we follow this trend, and propose a compact intermediate-energy storage ring light source to fill the gap between the third-generation light sources, SSRF and HLS-II, and the fourth-generation light sources (HEPS and HALF) in China, to meet most of the requests from the materials research users in SZLab.

This paper is organized as follows: Section 2 gives the linear optics design, which is followed by its nonlinear optics optimization in Section 3. The intra-beam scattering (IBS) and Touschek scattering effects are evaluated in Section 4. Finally, its photon performance with some typical insertion devices is given in Section 5.

## 2. Linear Optics Design

In order to achieve a low natural emittance while maintaining a high straight section ratio, we adopted the double double-bend achromat (DDBA) lattice [26], which has four bending magnets per cell and provides an additional straight section in the middle of the arc. The storage ring has an energy of 3 GeV and a circumference of 288 m, with a total of 12 cells. Each cell contains a long straight section (LSS) of 6.20 m and a short

straight section (SSS) of 1.86 m, allowing for the accommodation of more insertion devices (IDs). A standard 24 m cell contains main magnetic elements including four dipoles, ten quadrupoles and ten sextupoles. Six sextupoles are located within the dispersion bump for chromaticity correction and four harmonic sextupoles are located in the dispersion-free region to optimize its nonlinear performance. Figure 3 shows the linear optics of the DDBA cell, and the main parameters of the storage ring are presented in Table 1.

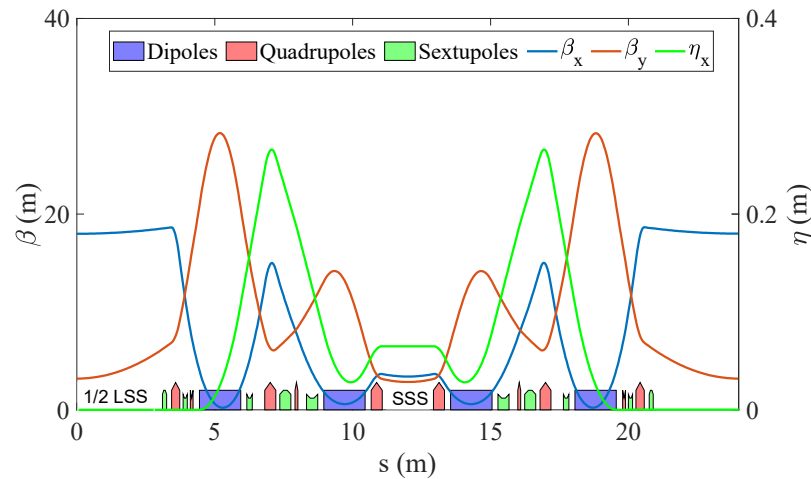


Figure 3. Optical functions of one DDBA cell.

Table 1. Ring parameters.

Parameter	Value
Beam energy	3 GeV
Circumference	288 m
Lattice type	12 × DBA
Tunes	21.17, 7.23
Horizontal emittance	2.57 nm rad
Energy spread	$8.64 \times 10^{-4}$
Natural chromaticity	−51.60, −30.45
Corrected chromaticity	1.0, 1.0
Momentum compaction factor	$8.23 \times 10^{-4}$
Energy loss per turn	0.625 MeV
Damping partition numbers	1.46, 1, 1.54
Damping time	6.33 ms, 9.22 ms, 5.97 ms
Long straight section	12 × 6.20 m
Short straight section	12 × 1.86 m
Twiss at LSS (betax, betay, etax)	18.0 m, 3.20 m, 0 m
Twiss at SSS (betax, betay, etax)	3.41 m, 2.85 m, 0.065 m
RF frequency	499.654 MHz
Harmonic number	480
RF voltage	4.0 MV
RF bucket height	4.06%
RMS bunch length	3.58 mm

There is only one family of combined dipole in the storage ring, with a dipole magnetic field of 0.87 T and a combined quadrupole field gradient of  $-5.27$  T/m. There are five families of quadrupoles used for focusing, with the maximum quadrupole strength being 24.33 T/m. The maximum sextupoles strength is 824.57 T/m<sup>2</sup>. The specifications of these magnets can be found in Table 2. The magnetic field strengths of these magnets are almost at the level of third-generation light source, and the requirements for the bore diameter of

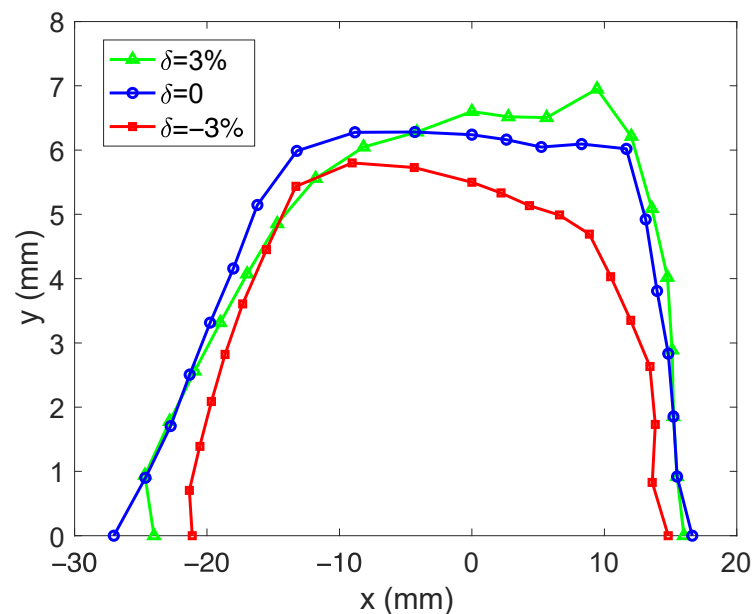
the magnets are much less stringent than for the DLSR. Therefore, the vacuum chamber of this DDBA ring can be made very large, which is conducive to reducing the impedance and provides very favorable conditions for the storage ring to achieve a high beam current, while the straight section of this DDBA lattice occupies a relatively high ratio, which facilitates the installation of a larger number of IDs.

**Table 2.** Specifications of main magnets.

Magnet	Name	Length	Strength	Bore Diameters
Combined dipoles	B	1.50 m	0.87 T, $-5.27$ T/m	-
Quadrupoles	Q1	0.30 m	22.37 T/m	50 mm
	Q2	0.10 m	$-7.37$ T/m	50 mm
	Q3	0.40 m	24.33 T/m	50 mm
	Q4	0.10 m	7.37 T/m	50 mm
	Q5	0.40 m	22.12 T/m	50 mm
Sextupoles	S1	0.15 m	$687.58$ T/m <sup>2</sup>	56 mm
	S2	0.15 m	$-824.57$ T/m <sup>2</sup>	56 mm
	SD1	0.20 m	$-368.87$ T/m <sup>2</sup>	56 mm
	SF	0.40 m	$430.02$ T/m <sup>2</sup>	56 mm
	SD2	0.40 m	$-483.10$ T/m <sup>2</sup>	56 mm

### 3. Nonlinear Optics Optimization

The DDBA lattice employs three families of sextupole magnets, namely SF, SD1, and SD2, for chromaticity correction, and two families of harmonic sextupole magnets, S1 and S2. Octupole magnets are not utilized, resulting in a total of three knobs for nonlinear optimization (SF, SD1 with fixed strength used for chromaticity correction). During optimization, we utilized the *OPA* code [27] to optimize the resonance driving terms (RDT) while fixing the corrected chromaticity to (1, 1). The optimized solutions were imported into the *Elegant* code [28] for tracking. Figure 4 shows the on- and off-momentum dynamics aperture (DA) in six dimensions (6D) at the injection point (at the center of LSS), including synchrotron radiation and RF cavity. The 6D DA is large and maintains no significant reduction even for off-momentum, making it highly suitable for off-axis injection.

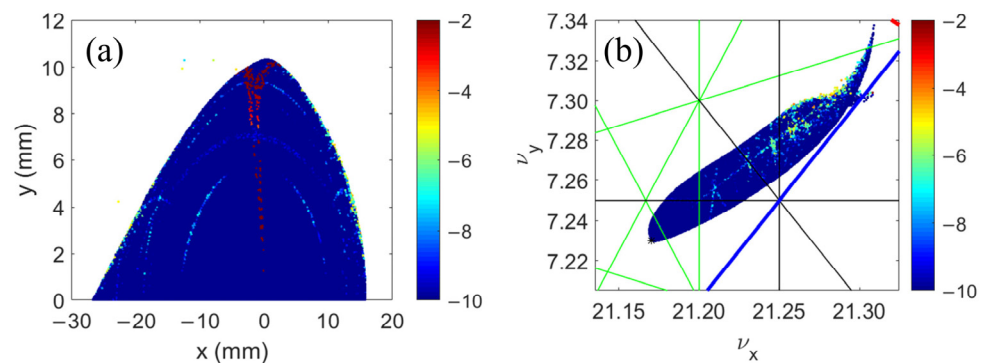


**Figure 4.** 6D DA of on- and off-momentum at the injection point (at the center of LSS).

Frequency map analysis (FMA) [29] was employed to analyze the DDBA lattice. FMA is a numerical method based on fine Fourier techniques, which provides a clear representation of the global dynamics of many multidimensional systems. FMA transforms the particle coordinate space  $(x, y)$  into the frequency space  $(\nu_x, \nu_y)$ , where regular motion appears as a fixed point and irregular motion diffuses, manifesting as changes in tunes with the number of turns. The diffusion rate is defined as the following formula:

$$D_r = \log_{10}\left(\frac{\sqrt{\Delta\nu_x^2 + \Delta\nu_y^2}}{N}\right), \quad (2)$$

where  $\Delta\nu_x$  and  $\Delta\nu_y$  are, respectively, the differences in  $x$  and  $y$  tunes from the first and second half of the tracking, and  $N$  is the number of turns. And a smaller  $D_r$  indicates more stable particle motion. Figure 5 displays the results of FMA, where particles were tracked for 1024 turns, and  $D_r$  was calculated based on the tunes from the first 512 turns and the last 512 turns. In Figure 5b, resonance lines up to the fifth order are plotted, with the blue lines representing second-order resonances, red lines representing third-order resonances, black lines representing fourth-order resonances, and green lines representing fifth-order resonances. From Figure 5b, it can be found that the particles do not cross any potentially dangerous resonance lines, which indicates that the lattice has good nonlinear dynamics performance.



**Figure 5.** FMA of the optimized DA, tracked for 1024 turns: (a)  $x$ - $y$  space, (b) tune space. The color bar represents the diffusion rate. Blue color denotes more regular motion and red color more chaotic.

Figure 6 demonstrates the tune shift with momentum deviation ranging from  $-8\%$  to  $8\%$ . It can be seen that the vertical tune of the lattice crosses the half-integer resonance when the momentum deviation approaches  $-8\%$ . Combined with the FMA results of off-momentum shown in Figure 7, it can be observed that no particle loss occurs when crossing the half-integer resonance [30], indicating that the lattice has good momentum acceptance and excellent off-momentum dynamics. We also performed 4D and 6D tracking for the local momentum aperture (LMA), and the results are presented in Figure 8. It can be seen that the 4D LMA is very large, with a momentum acceptance of approximately  $11\%$  at the injection LSS. However, the 6D tracking of the LMA is limited by the RF acceptance, which is approximately  $4\%$ . Such a large LMA is very favorable for the beam's Touschek lifetime [31], and we will discuss the Touschek lifetime of the beam after considering the IBS effect in the next section.

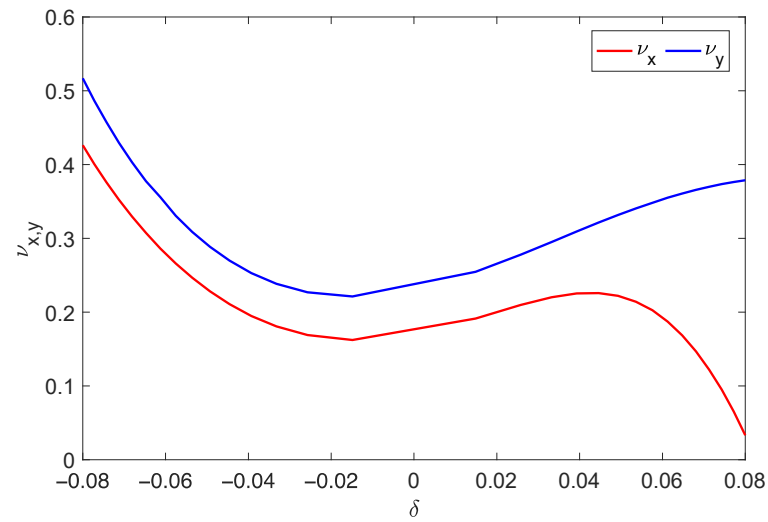


Figure 6. Momentum dependent tune shift.

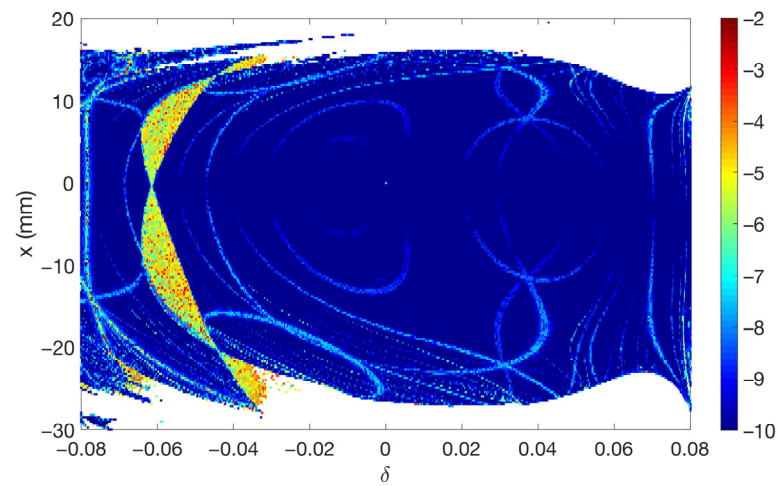


Figure 7. Off-momentum FMA. The color bar represents the diffusion rate. Blue color denotes more regular motion and red color more chaotic.

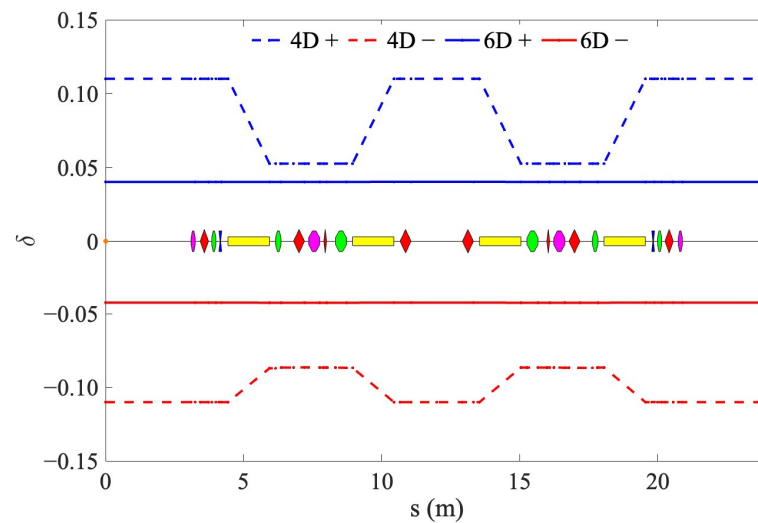
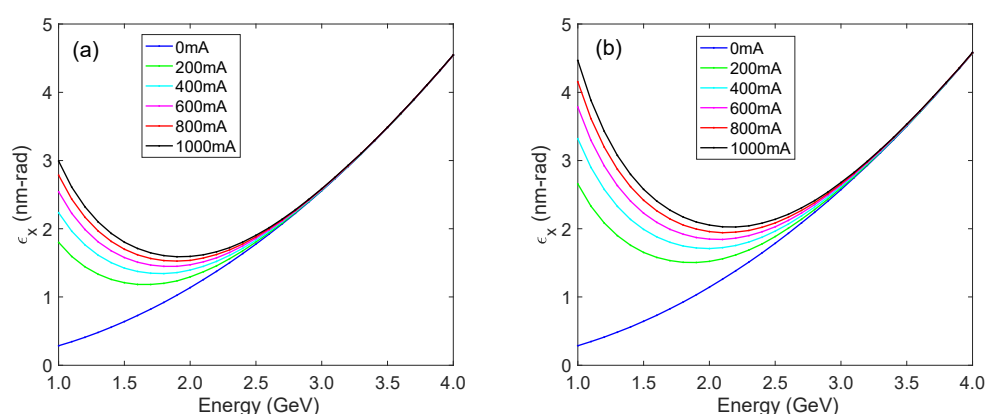


Figure 8. LMA of one cell. The yellow rectangle represents the dipoles, the red and blue shapes represent the quadrupoles, and the magenta and green shapes represent the sextupoles.

#### 4. Intra-Beam Scattering (IBS) and Touschek Scattering

The IBS effect is caused by small-angle Coulomb scattering between charged particles in a bunch [32,33]. It is generally more severe in MBA lattices due to ultra-low emittance, which leads to a high density of electron bunches. This results in severe IBS effects, subsequently increasing the emittance and energy spread of the beam in its final equilibrium state. To decrease the natural emittance of the storage ring, the MBA lattice usually designs the bending magnets with weak fields. This results in smaller synchrotron radiation losses and longer damping times. The IBS effect is closely related to the damping time, and the longer the damping time, the more severe the IBS effect. For a specific lattice structure, the natural emittance of the beam is proportional to the square of its energy, while the IBS growth rate is inversely proportional to the cube of its energy. Therefore, under the combined effects of IBS, synchrotron radiation damping, and quantum excitation, there exists an optimized energy value at which the equilibrium emittance of the storage ring is minimized.

The relationship between beam energy and equilibrium emittance under different beam currents was simulated based on the storage ring parameters presented in Table 1. The IBS effect of this DDBA lattice was simulated in 80% bunch filling mode with 1% and 0.1% transverse coupling, respectively, using the Elegant code to calculate the IBS effect, and the results are shown in Figure 9. As can be seen in Figure 9, the minimum equilibrium emittance of the DDBA lattice occurs at a beam energy of approximately 1.5–2.0 GeV as the beam current increases at the transverse coupling of 1%. At the transverse coupling of 0.1%, the minimum equilibrium emittance of the DDBA lattice occurs at a beam energy of about 1.8–2.2 GeV as the beam current increases. At lower beam energies, the equilibrium emittance is primarily determined by the combined effects of synchrotron radiation damping and IBS effect due to the small horizontal emittance and high IBS growth rate. At higher energies, the equilibrium emittance is primarily determined by quantum excitation and synchrotron radiation damping, which is approximately equal to the natural emittance of the beam at zero beam current. In this paper, we selected a beam energy of 3 GeV because, at this energy, the IBS effect is negligible, and it is suitable for producing hard X-rays. Due to the low magnet strength of this DDBA lattice, the ability to boost the beam energy of this storage ring to 4 GeV is retained for subsequent upgrades.

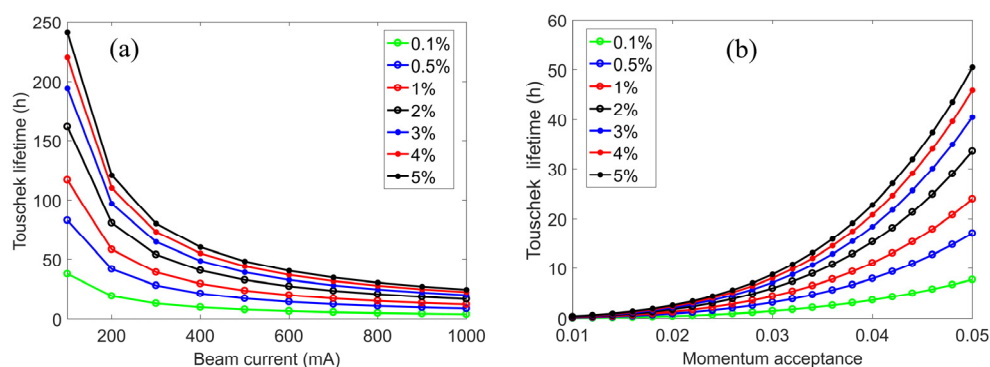


**Figure 9.** Equilibrium emittance versus beam energy for different beam currents at (a) 1% transverse coupling; (b) 0.1% transverse coupling.

Touschek scattering is a large-angle elastic scattering process between electrons inside a bunch. The Touschek effect is related to IBS, but specifically refers to scattering events that result in a significant transfer of momentum from the transverse to the longitudinal planes. In contrast, IBS refers to multiple small-angle scattering events. If the change in



longitudinal momentum is significant, the momentum deviation of one or both electrons may exceed the momentum acceptance of the storage ring, resulting in the loss of electrons from the bunch. In low-emittance storage rings, Touschek scattering is the primary factor that limits beam lifetime. We calculated and analyzed the Touschek lifetime of the beam for various beam currents, transverse couplings, and momentum acceptances, and the findings are presented in Figure 10. For Figure 10a, the momentum acceptance of the storage ring was set to a fixed value of 4.06% in the calculation, which is consistent with the nonlinear dynamics performance of the designed DDBA lattice, as shown in Figure 8. For Figure 10b, the beam current was fixed at 1000 mA in the calculation. The RF acceptance is about 5.26% when the RF voltage is 6.1 MV. We analyze the Touschek lifetime by restricting the maximum value of momentum aperture to 5%, i.e., not more than the minimum value of LMA in Figure 8.



**Figure 10.** Touschek lifetime versus beam current for different transverse couplings (a); Touschek lifetime versus momentum acceptance for different transverse couplings (b).

The brilliance of a storage ring light source is proportional to the beam current and inversely proportional to the product of the horizontal and vertical emittances, where the horizontal emittance is determined by the lattice structure and the beam current is limited by instability thresholds. Therefore, third-generation storage ring light sources generally increase the brilliance of the light source by reducing the vertical emittance. However, this approach can decrease the Touschek lifetime of the beam. Magnet alignment and transverse coupling correction can reduce the vertical emittance of the storage ring to the quantum limit [34]. Due to its small horizontal emittance, the DLSR has a very low Touschek lifetime. Therefore, the DLSR is typically operated at full coupling to increase the Touschek lifetime. In this DDBA lattice, with a transverse coupling of only 0.1% and a beam current of 1000 mA, the Touschek lifetime remains at 3.74 h. This is sufficient for Top-up operation, demonstrating that the DDBA lattice can operate at very low transverse coupling. We investigated the Touschek lifetime under larger transverse coupling. At 2% coupling with a beam current of 1000 mA, the Touschek lifetime is about 16.17 h, consistent with that of a general third-generation light source operating under a beam current of about 200 mA. If the DDBA lattice operates at 5% coupling at 1000 mA, its Touschek lifetime is as high as 24.09 h. The DDBA lattice has a high Touschek lifetime in either case.

## 5. Photon Performance

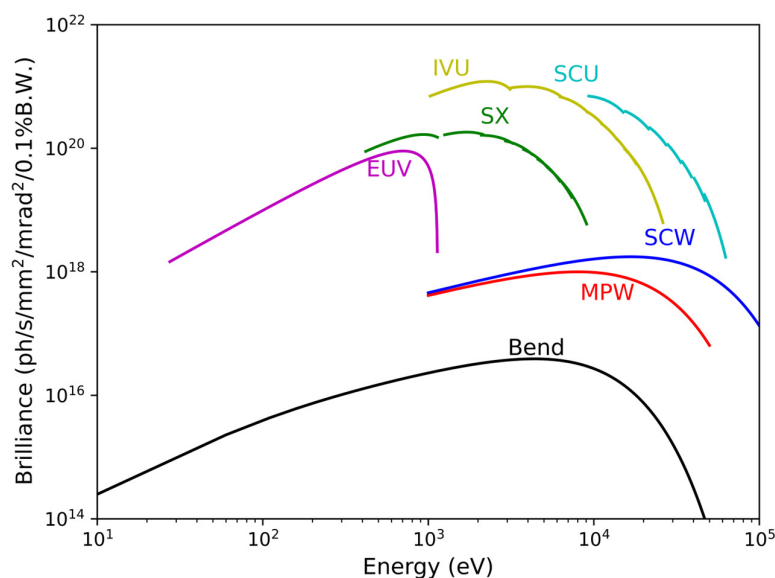
Initially, five types of insertion devices (IDs), which include in-vacuum undulators (IVU), multiple wigglers (MPW), APPLE-II type elliptically polarized undulators (EPUs), superconducting (SC) wigglers, and SC undulators, will be adopted to cover the whole energy range from extreme-ultraviolet (EUV) to hard X-ray. The typical parameters of these IDs are summarized in Table 3. Brilliances of these IDs, calculated using the code

SPECTRA [35], are shown in Figure 11. The brilliance of third-generation storage rings is typically in the order of  $10^{20}$  ph/s/mm<sup>2</sup>/mrad<sup>2</sup>/0.1%BW, and the brilliance of the DLSR is normally in the order of  $10^{22}$  ph/s/mm<sup>2</sup>/mrad<sup>2</sup>/0.1%BW. From Figure 11, it can be seen that the design in this paper can reach the  $10^{21}$  ph/s/mm<sup>2</sup>/mrad<sup>2</sup>/0.1%BW, which is between the third-generation storage rings and the DLSRs.

**Table 3.** Typical parameters of planned IDs.

ID Type	Period (mm)	Number Periods	Max B(T)
IVU	22	190	1.15
MPW	100	13	1.6
Apple-II (EUV)	75	53	1.08
Apple-II (SX *)	56	71	0.44
SC wiggler	48	22	4.2
SC undulator	10	116	2.0

\*SX: soft X-ray.



**Figure 11.** Brilliance of planned IDs.

## 6. Discussions and Conclusions

Most DLSRs, in operation, under construction, or in the planning phase, that adopt a hybrid MBA or HOA MBA structure normally require magnets with very high magnetic field strength. Although stronger focusing can reduce the emittance of the electron beam and thus increase the brilliance of X-rays, it inevitably reduces the aperture of the vacuum chamber, which is not favorable for achieving high current operation. Furthermore, the DA and MA of the MBA lattice are generally small, which poses great challenges to the beam injection and Touschek lifetime.

Based on the emerging DDBA lattice structure, the design of very compact intermediate-energy storage ring light sources to fill the gap between the third-generation and fourth-generation light sources in China is given, to serve as a dedicated X-ray light source for the materials research in SZLab, a newly established research institute in Suzhou, China.

By using advanced insertion device technologies, which include IVU, MPW, APPLE-II type EPUs, SC wigglers, and SC undulators, we are expecting high photon performances to fulfill the diverse requirements of most users from the material science communities, e.g., structural materials, energy materials, information and communication technology materials, and some frontier functional materials, to name a few.

**Author Contributions:** Conceptualization, C.L. and J.C.; methodology, C.L.; software, C.L. and H.W.; validation, C.L., J.C. and Q.Z.; formal analysis, C.L.; investigation, C.L., H.W. and K.W.; resources, J.C.; data curation, C.L. and H.W.; writing—original draft preparation, C.L.; writing—review and editing, C.L., J.C., H.W., Q.Z. and K.W.; project administration, J.C.; funding acquisition, C.L. and J.C. All authors have read and agreed to the published version of the manuscript.

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