

Covariance Symmetries Detection in PolInSAR Data

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Abstract—In the last two decades, the use of synthetic aperture radar (SAR) for remote sensing purposes has significantly developed due to improvements in the quality and the availability of the images. Two powerful SAR techniques, namely, polarimetry and interferometry, have further increased the range of applications of the sensed data. Using polarimetry, geometrical properties and geophysical parameters, such as shape, roughness, texture, and moisture content, can be retrieved with considerable accuracy, while interferometric information may be used to extract vertical information with accuracy less than 1 cm. In this paper, the potential of using joint polarimetry and interferometry techniques in SAR data (PolInSAR) for the purpose of SAR image classification is investigated. To achieve this goal, we extend a covariance symmetry detection framework to the PolInSAR scenario. The proposed approach will be shown to be able to exploit the peculiar structures of the covariance matrices of PolInSAR images to discriminate structures within the image. Results using real-SAR data are presented to validate the effectiveness of the proposed approach.

Index Terms—Azimuth symmetry, cross covariance, detection, polarimetric interferometry, PolInSAR, reflection symmetry, rotation symmetry, symmetries.

I. INTRODUCTION

POLARIMETRIC interferometry is a recent technique, [1] which uses two spatially shifted polarimetric antennas allowing the measurement of the coherence associated with the various polarimetric channels as well as the height of the polarimetric phase centers. The potential of this technique for the extraction of physical parameters from vegetation, ice, and urban areas has been validated on various data sets and is still being evaluated on other types of data acquired at high resolution by airborne systems [2]–[4]. The polarimetric scattering phenomenon of a medium can be described completely using a (3×3) matrix formulation, namely, the covariance matrix [5]. In general, the medium encountered exhibits symmetric properties, for example, the forest canopy layer, which consists of randomly oriented leaves twigs and branches, exhibits usually

Manuscript received January 18, 2018; revised April 21, 2018; accepted May 30, 2018. The work of J. J. Soraghan and C. Clemente was supported in part by the Engineering and Physical Sciences Research Council under Grant EP/K014307/1 and in part by the MOD University Defence Research Collaboration in Signal Processing. (*Corresponding author: Sofiane Tahraoui.*)

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Digital Object Identifier 10.1109/TGRS.2018.2845881

azimuthal symmetry [6], while an agricultural field ploughed in the direction parallel to the flight path has a reflection symmetry [7]; finally, an elliptical scatterer is a general example of rotation symmetry [7]. The form of the covariance matrices is related to the medium symmetries, which makes it detectable. However, the backscattered signal from natural sources, such as forests and high-altitude vegetation, is always a mixture of responses from the vegetation volume and the underlying ground [8], particularly in forest areas, where target scattering space expands in height. This means that the scattering is a combination of all vertical elementary scatterers. This phenomenon does not allow differentiation between symmetry sources, for example, it is not possible to state if a detected azimuth symmetry originates at the ground level due to the vegetation or is due to the canopy contribution. Thus, a technique is required that is able to discriminate between the different contributions. The use of polarimetric synthetic aperture radar interferometry instead of just polarimetric SAR (Pol-SAR) represents a potential solution to this challenge, since it enables the estimation of elevation in each resolution cell.

The purpose of this paper is to extend the framework developed in [9] for the detection of covariance symmetries in polarimetry and interferometry techniques in SAR data (PolInSAR). Precisely, both the radar returns of the PolInSAR scenario and the strategy for symmetries detection are modeled. Compared with the work presented in [9], this framework enhances the capability of detecting covariances not only in 2-D but also in a 3-D space. The proposed analytical framework differs from that of [9], as it accounts for peculiar characteristics of the PolInSAR covariance matrices as well as thanks to its capabilities to provide a novel tool for advanced remote sensing applications. An example of the latter consists in integrating the proposed approach in an enhanced H-A- α [10], [11] PolInSAR decomposition in order to extract different classes containing both the symmetry and elevation information. The proposed framework is validated on real-SAR data, demonstrating that more information can be extracted from the PolInSAR data compared with the polarimetric data only.

The remainder of this paper is organized as follows. Section II introduces the basic concept of Pol-SAR interferometry and describes its symmetric target properties. The proposed framework for detecting covariance symmetries in PolInSAR is developed in Section III. The performance of the proposed technique applied both on simulated and real L-band SAR data is presented and discussed in Section IV. Finally, some remarks are given before we conclude this paper.

II. SYMMETRIC TARGET PROPERTIES

In monostatic PolInSAR systems, the imaging area is scanned at least twice from slightly different angles. As a result, the system produces one master image and a relative scattering matrix, and several slave images and related scattering matrices [12], [13]. The simpler scenario is represented when only one slave image is generated and is called bis-canning system yielding to two scattering matrices [14], [15], namely, \mathbf{S}_m and \mathbf{S}_s , where the subscript m stands for master and s stands for slave

$$\mathbf{S}_m = \begin{bmatrix} S_{hh_m} & S_{hv_m} \\ S_{vh_m} & S_{vv_m} \end{bmatrix} \quad \mathbf{S}_s = \begin{bmatrix} S_{hh_s} & S_{hv_s} \\ S_{vh_s} & S_{vv_s} \end{bmatrix}. \quad (1)$$

The subscripts hh, vv, hv, and vh identify the transmitter/receiver Pol-SAR channels.

The complete scattering phenomenon representing one resolution cell can be described using a (6×6) covariance matrix \mathbf{C}_6 formed using the superposition of the scattering vectors \vec{k}_m and \vec{k}_s obtained in turn by vectorization of (1) under the conventional linear basis as

$$\vec{k}_m = \frac{1}{\sqrt{2}} \begin{pmatrix} S_{hh_m} \\ \sqrt{2}S_{hv_m} \\ S_{vv_m} \end{pmatrix} \quad \vec{k}_s = \frac{1}{\sqrt{2}} \begin{pmatrix} S_{hh_s} \\ \sqrt{2}S_{hv_s} \\ S_{vv_s} \end{pmatrix}. \quad (2)$$

Thus, the covariance matrix \mathbf{C}_6 formed using the superposition of those scattering vectors can be written as

$$\mathbf{C}_6 = \left\langle \begin{bmatrix} \vec{k}_m \\ \vec{k}_s \end{bmatrix} \begin{bmatrix} \vec{k}_m^H & \vec{k}_s^H \end{bmatrix} \right\rangle$$

the extended version of \mathbf{C}_6 is reported in (3), as shown at the bottom of this page, where \mathbf{C}_{11} and \mathbf{C}_{22} are the 3×3 conventional Hermitian polarimetric covariance matrices that describe the polarimetric properties of each image separately and \mathbf{C}_{12} and/or \mathbf{C}_{21} is the 3×3 cross-covariance matrix that contains not only polarimetric information but also information

related to the interferometric phases of different polarization channels.

When the medium exhibits symmetric properties, these polarimetric matrices (i.e., \mathbf{C}_{11} or \mathbf{C}_{22}), and PolInSAR matrices (i.e., \mathbf{C}_{12} and \mathbf{C}_{21}), show a particular structure [7], [16]. These matrices contain a rich amount of information allowing us to analyze targets symmetry types. Moreover, the use of the cross-covariance matrix enables us to localize in the vertical direction the detected symmetries. Hence, the starting point is the definition of the cross-correlation matrix in the presence of a reciprocal medium [5], [17] (4).

$$\mathbf{C}_{int} = \begin{bmatrix} \langle S_{hh_m} S_{hh_s}^* \rangle & \sqrt{2} \langle S_{hh_m} S_{hv_s}^* \rangle & \langle S_{hh_m} S_{vv_s}^* \rangle \\ \sqrt{2} \langle S_{hv_m} S_{hh_s}^* \rangle & 2 \langle S_{hv_m} S_{hv_s}^* \rangle & \sqrt{2} \langle S_{hv_m} S_{vv_s}^* \rangle \\ \langle S_{vv_m} S_{hh_s}^* \rangle & \sqrt{2} \langle S_{vv_m} S_{hv_s}^* \rangle & \langle S_{vv_m} S_{vv_s}^* \rangle \end{bmatrix} \quad (4)$$

It is important to note that while \mathbf{C}_6 is Hermitian semidefinite positive by definition, \mathbf{C}_{int} is not. Among the vast number of forms that this matrix can exhibit, it is desirable to detect canonical structures related to known properties of symmetry.

The phase difference between the master and the slave is caused by the difference in the path [1], [18], [19] of the wave as well as to the temporal change between the two acquisitions (i.e., the master and the slave phases) [20]. In our case, we ignore the effect of the latter and suppose null temporal baseline.

In the following, we will describe how different phase contributions operate in PolInSAR.

Let us denote by S the polarimetric scattering coefficient, with p and q representing one of the possible transmitter and receiver polarizations (H or V), respectively.

$$\mathbf{C}_6 = \begin{bmatrix} \underbrace{\begin{pmatrix} \langle S_{hh_m} S_{hh_m}^* \rangle & \sqrt{2} \langle S_{hh_m} S_{hv_m}^* \rangle & \langle S_{hh_m} S_{vv_m}^* \rangle \\ \sqrt{2} \langle S_{hv_m} S_{hh_m}^* \rangle & 2 \langle S_{hv_m} S_{hv_m}^* \rangle & \sqrt{2} \langle S_{hv_m} S_{vv_m}^* \rangle \\ \langle S_{vv_m} S_{hh_m}^* \rangle & \sqrt{2} \langle S_{vv_m} S_{hv_m}^* \rangle & \langle S_{vv_m} S_{vv_m}^* \rangle \end{pmatrix}}_{\mathbf{C}_{11}} & \underbrace{\begin{pmatrix} \langle S_{hh_m} S_{hh_s}^* \rangle & \sqrt{2} \langle S_{hh_m} S_{hv_s}^* \rangle & \langle S_{hh_m} S_{vv_s}^* \rangle \\ \sqrt{2} \langle S_{hv_m} S_{hh_s}^* \rangle & 2 \langle S_{hv_m} S_{hv_s}^* \rangle & \sqrt{2} \langle S_{hv_m} S_{vv_s}^* \rangle \\ \langle S_{vv_m} S_{hh_s}^* \rangle & \sqrt{2} \langle S_{vv_m} S_{hv_s}^* \rangle & \langle S_{vv_m} S_{vv_s}^* \rangle \end{pmatrix}}_{\mathbf{C}_{12}} \\ \underbrace{\begin{pmatrix} \langle S_{hh_s} S_{hh_m}^* \rangle & \sqrt{2} \langle S_{hh_s} S_{hv_m}^* \rangle & \langle S_{hh_s} S_{vv_m}^* \rangle \\ \sqrt{2} \langle S_{hv_s} S_{hh_m}^* \rangle & 2 \langle S_{hv_s} S_{hv_m}^* \rangle & \sqrt{2} \langle S_{hv_s} S_{vv_m}^* \rangle \\ \langle S_{vv_s} S_{hh_m}^* \rangle & \sqrt{2} \langle S_{vv_s} S_{hv_m}^* \rangle & \langle S_{vv_s} S_{vv_m}^* \rangle \end{pmatrix}}_{\mathbf{C}_{21}} & \underbrace{\begin{pmatrix} \langle S_{hh_s} S_{hh_s}^* \rangle & \sqrt{2} \langle S_{hh_s} S_{hv_s}^* \rangle & \langle S_{hh_s} S_{vv_s}^* \rangle \\ \sqrt{2} \langle S_{hv_s} S_{hh_s}^* \rangle & 2 \langle S_{hv_s} S_{hv_s}^* \rangle & \sqrt{2} \langle S_{hv_s} S_{vv_s}^* \rangle \\ \langle S_{vv_s} S_{hh_s}^* \rangle & \sqrt{2} \langle S_{vv_s} S_{hv_s}^* \rangle & \langle S_{vv_s} S_{vv_s}^* \rangle \end{pmatrix}}_{\mathbf{C}_{22}} \end{bmatrix} \quad (3)$$

- 1) *Identical Polarization in Transmission/Reception*: When using identical polarization in transmission and reception, the only phase component is a combination between the master and the slave phases φ_{int} as shown in (8) and (9)

$$S_{\text{pp}_m} = |S_{\text{pp}_m}| e^{j\varphi_{\text{pp}_m}} \quad S_{\text{pp}_s} = |S_{\text{pp}_m}| e^{j\varphi_{\text{pp}_s}} \quad (5)$$

where

$$\varphi_{\text{pp}_m} = -\frac{4\pi R_m}{\lambda} + \varphi_{\text{scr}} \quad (6)$$

and

$$\varphi_{\text{pp}_s} = -\frac{4\pi R_s}{\lambda} + \varphi_{\text{scr}} = -\frac{4\pi(R_m + \delta R)}{\lambda} + \varphi_{\text{scr}} \quad (7)$$

R_m and R_s are the geometric distances and φ_{scr} is the proper phase of the scatterer in the same resolution cell (i.e., same scatterer). So, the interferometric phase can be written as

$$\varphi_{\text{int}} = \varphi_{\text{pp}_m} - \varphi_{\text{pp}_s} = -\frac{4\pi\delta R}{\lambda} \quad (8)$$

and

$$\begin{aligned} \langle S_{\text{pp}_m} S_{\text{pp}_s} \rangle &= |S_{\text{pp}_m}| |S_{\text{pp}_m}| e^{j\varphi_{\text{int}}} \\ \langle S_{\text{pp}_m} S_{\text{qq}_s} \rangle &= |S_{\text{pp}_m}| |S_{\text{qq}_m}| e^{j\varphi_{\text{int}}}. \end{aligned} \quad (9)$$

- 2) *Different Polarizations in Transmission/Reception Only in Master or Only in Slave*: In case of using different polarizations between transmission and reception, an additional phase component τ_{pq} linked to a polarization phase shift between p and q is added as shown in (10), and this component appears in (11)

$$\begin{aligned} S_{\text{pq}_m} &= |S_{\text{pp}_m}| e^{-j\frac{4\pi R_m + \tau_{pq}}{\lambda} + \varphi_{\text{scr}}} \\ S_{\text{pq}_s} &= |S_{\text{pp}_m}| e^{-j\frac{4\pi R_m + \delta R + \tau_{pq}}{\lambda} + \varphi_{\text{scr}}} \end{aligned} \quad (10)$$

$$\begin{aligned} \langle S_{\text{pp}_m} S_{\text{pq}_s} \rangle &= |S_{\text{pp}_m}| |S_{\text{pq}_m}| e^{j\varphi_{\text{int}} + \varphi_{pq}} \\ \langle S_{\text{pq}_m} S_{\text{pp}_s} \rangle &= |S_{\text{pp}_m}| |S_{\text{pq}_m}| e^{j\varphi_{\text{int}} - \varphi_{pq}}. \end{aligned} \quad (11)$$

- 3) *Different Polarizations in Transmission/Reception in Master and Slave Acquisitions*: In this case, the additional phase component τ_{pq} will be compensated and vanishes as in

$$\begin{aligned} \langle S_{\text{pq}_m} S_{\text{pq}_s} \rangle &= |S_{\text{pq}_m}| |S_{\text{pq}_m}| e^{j\varphi_{\text{int}}} \\ \langle S_{\text{qp}_m} S_{\text{pq}_s} \rangle &= |S_{\text{qp}_m}| |S_{\text{pq}_m}| e^{j\varphi_{\text{int}}}. \end{aligned} \quad (12)$$

Hereafter, we review the general cross-covariance matrix (i.e., \mathbf{C}_{12} and \mathbf{C}_{21}) when symmetry properties are predominant on the target in view. Note that the phase center of the volume scattering will be assumed to be the same for all polarizations [8]. And for analytic purposes, we will assume that

$$|S_{\text{hh}_m}| = |S_{\text{hh}_s}| \quad |S_{\text{vv}_m}| = |S_{\text{vv}_s}|. \quad (13)$$

In the following, each case of symmetry will be represented by its cross-covariance matrix, taking into account the inherent interferometric information.

A. Reflection Symmetry

Let us consider an agricultural field ploughed in the direction parallel to the flight line. Such a medium exhibits a reflection symmetry along the propagation direction plane and the h polarization direction. In such a situation, the correlation between the copolarized and the cross-polarized elements is forced to be null, leading to the following form of the covariance and cross-covariance matrices $\mathbf{C}_{\text{int}}^{rf}$ [7] [see (14)].

$$\mathbf{C}_{\text{int}}^{rf} = \begin{bmatrix} \langle S_{\text{hh}_m} S_{\text{hh}_s}^* \rangle & 0 & \langle S_{\text{hh}_m} S_{\text{vv}_s}^* \rangle \\ 0 & 2\langle S_{\text{hv}_m} S_{\text{hv}_s}^* \rangle & 0 \\ \langle S_{\text{vv}_m} S_{\text{hh}_s}^* \rangle & 0 & \langle S_{\text{vv}_m} S_{\text{vv}_s}^* \rangle \end{bmatrix} \quad (14)$$

This result is valid for volume scattering, surface scattering, or volume–surface interactions for all scattering orders no matter how dense the medium or how rough the surface. In particular, it is valid as long as the scattering configuration has the reflection symmetry [5], [7], [9]. Let us consider a permutation matrix \mathbf{U} , i.e.,

$$\mathbf{U} = \begin{bmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 1. \end{bmatrix} \quad (15)$$

This matrix permits us to transform $\mathbf{C}_{\text{int}}^{rf}$ as

$$\begin{aligned} \mathbf{C}_{\text{int}}^{rf} &= \mathbf{U} \mathbf{C}_{\text{int}}^{ref} \mathbf{U}^H \\ &= \begin{bmatrix} 2\langle S_{\text{hv}_m} S_{\text{hv}_s}^* \rangle & 0 & 0 \\ 0 & \langle S_{\text{hh}_m} S_{\text{hh}_s}^* \rangle & \langle S_{\text{hh}_m} S_{\text{vv}_s}^* \rangle \\ 0 & \langle S_{\text{vv}_m} S_{\text{hh}_s}^* \rangle & \langle S_{\text{vv}_m} S_{\text{vv}_s}^* \rangle \end{bmatrix} \\ &= \begin{bmatrix} \mathbf{a} & 0 \\ 0 & \mathfrak{C}_{\text{int}}^1 \end{bmatrix} \end{aligned} \quad (16)$$

where

$$\mathfrak{C}_{\text{int}}^1 = \begin{bmatrix} |S_{\text{hh}_m}| |S_{\text{hh}_m}| e^{j\varphi_{\text{int}}} & |S_{\text{hh}_m}| |S_{\text{vv}_m}| e^{j\varphi_{\text{int}}} \\ |S_{\text{hh}_m}| |S_{\text{vv}_m}| e^{j\varphi_{\text{int}}} & |S_{\text{vv}_m}| |S_{\text{vv}_m}| e^{j\varphi_{\text{int}}} \end{bmatrix} \quad (17)$$

and

$$\mathbf{a} = 2|S_{\text{hv}_m}| |S_{\text{hv}_m}| e^{j\varphi_{\text{int}}}. \quad (18)$$

Under the assumption (13), $\mathfrak{C}_{\text{int}}^1$ is a symmetric matrix and \mathbf{a} is a complex number containing the vertical position information.

B. Rotation Symmetry

The rotation symmetry is characterized by a covariance matrix invariance under the rotation around an axis by any considered angle [5]. Denoting by

$$\mathfrak{T} = \begin{bmatrix} \frac{1}{\sqrt{2}} & 0 & \frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{2}} & 0 & -\frac{1}{\sqrt{2}} \\ 0 & 1 & 0 \end{bmatrix} \quad (20)$$

a transition matrix from covariance to coherence (note that the two representations are equivalent and contain the same information) and by

$$\mathbf{V} = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & j \\ 1 & 0 & 0 \end{bmatrix} \quad (21)$$

a complex permutation matrix, allowing us to model \mathbf{C}_{int}^{rot} as

$$\mathbf{T}_{Sm}^{rot} = \mathbf{V} \mathbf{\Xi} \mathbf{C}_{int}^{rot} \mathbf{\Xi}^H \mathbf{V}^H = \begin{bmatrix} \mathbb{T}_{int}^2 & 0 \\ 0 & \mathbf{b} \end{bmatrix} \quad (22)$$

where

$$\mathbb{T}_{int} = 2e^{j\varphi_{int}} \begin{bmatrix} E_{11} & E_{22} \\ E_{22} & E_{11} \end{bmatrix} \quad (23)$$

where

$$\begin{aligned} E_{11} &= |S_{hv_m}| |S_{hv_s}| \\ E_{22} &= |S_{hh_m}| |S_{hv_s}| e^{j(\varphi_{hv} - \pi/2)}. \end{aligned}$$

Thus, \mathbb{T}_{int} is a centrosymmetric matrix and $\mathbf{b} = |S_{hh_m}|(|S_{hh_s}| + |S_{vv_s}|)e^{j\varphi_{int}}$ is a complex number.¹

C. Azimuth Symmetry

The azimuth symmetry arises as the combination of a rotation with reflection symmetries in any plane that contains the rotation symmetry axis. Thus, the PolInSAR cross-covariance matrix in this case can be written as in (24), as shown at the bottom of this page.

In addition, its corresponding coherence matrix is

$$\mathbf{T}_{Sm}^{Az} = \mathbf{\Xi} \mathbf{C}_{int}^{Az} \mathbf{\Xi}^H = \begin{bmatrix} \mathbf{c} & 0 & 0 \\ 0 & \mathbf{d} & 0 \\ 0 & 0 & \mathbf{d} \end{bmatrix} \quad (25)$$

where $\mathbf{c} = |S_{hh_m}|(|S_{hh_s}| + |S_{vv_s}|)e^{j\varphi_{int}}$ and $\mathbf{d} = 2|S_{hv_m}| |S_{hv_s}| e^{j\varphi_{int}}$ are both complex numbers containing the vertical position information.

¹A centrosymmetric matrix is a matrix which is symmetric about its center. In particular, it means that the entries of the matrix satisfy the condition $\mathbb{T}_{int} = J \mathbb{T}_{int} J$. Where J is an $n \times n$ permutation matrix with ones on the secondary diagonal and zeros elsewhere.

III. TARGET SYMMETRY DETECTION

At this point, we have to define multiple hypotheses associated with each of the previously discussed symmetries. Let us consider the following hypotheses.

H_1 : No symmetry.

H_2 : Reflection symmetry.

H_3 : Rotation symmetry.

H_4 : Azimuth symmetry.

As proposed in [17] and [21], we consider a complex multivariate normal distribution with zero mean for N -looks 3-D observable random complex vectors $\vec{\mathbf{Z}}_{obs}$ i.e.,

$$\vec{\mathbf{Z}}_{obs} = (S_{hh} \quad \sqrt{2}S_{hv} \quad S_{vv})^T \quad (26)$$

as

$$f(\vec{\mathbf{Z}}_{obs} | \mathbf{C}) = \frac{1}{\pi^{3N} |\mathbf{C}|^N} \exp\{-\text{tr}(\mathbf{C}^{-1} \mathbf{S}_0)\} \quad (27)$$

where $|\cdot|$ denotes the determinant, $\text{tr}(\cdot)$ denotes the trace of the matrix, and $\mathbf{S}_0 = [\vec{\mathbf{Z}}_m \vec{\mathbf{Z}}_s^H]$. Each one of the four classes (i.e., H_1 , H_2 , H_3 , and H_4) has its specific characteristics. We shall call it the symmetry class and will be denoted as \mathbf{C}_{sym} . The maximum likelihood (ML) estimate of \mathbf{C}_{sym} can be obtained as the optimal solution to the optimization problem, i.e., (19) shown at the bottom of this page

$$\begin{aligned} \max_{\mathbf{C}} (\log(f(\vec{\mathbf{Z}}_{obs} | \mathbf{C}))) &= -N \min_{\mathbf{C}} [\log |\mathbf{C}| \\ &\quad + \text{tr}(\mathbf{C}^{-1} \mathbf{S})] - 3N \log \pi \end{aligned} \quad (28)$$

where $\mathbf{S} = \mathbf{S}_0/N$.

The third term on the right-hand side of (28) and the factor N can be ignored, because they do not affect the pixel classification. Thus, the optimal value is obtained by using

$$\min_{\mathbf{C}} [\log |\mathbf{C}| + \text{tr}(\mathbf{C}^{-1} \mathbf{S})] \quad (29)$$

and the optimal solution $\hat{\mathbf{C}}_{sym}$ for the previous classes are, respectively, given by the following.

H_1 : $\log |\mathbf{S}| + 3$ where $\hat{\mathbf{C}}_{sym} = \mathbf{S}$.

$$\mathbf{C}_{int}^{rt} = \begin{bmatrix} \langle S_{hh_m} S_{hh_s}^* \rangle & \sqrt{2} \langle S_{hh_m} S_{hv_s}^* \rangle & \langle S_{hh_m} S_{hh_s}^* \rangle - 4 \langle S_{hv_m} S_{hv_s}^* \rangle \\ -\sqrt{2} \langle S_{hh_m} S_{hv_s}^* \rangle & 2 \langle S_{hv_m} S_{hv_s}^* \rangle & \sqrt{2} \langle S_{hh_m} S_{hv_s}^* \rangle \\ \langle S_{hh_m} S_{hh_s}^* \rangle - 4 \langle S_{hv_m} S_{hv_s}^* \rangle & -\sqrt{2} \langle S_{hh_m} S_{hv_s}^* \rangle & \langle S_{hh_m} S_{hh_s}^* \rangle \end{bmatrix} \quad (19)$$

$$\mathbf{C}_{int}^{Az} = \begin{bmatrix} \langle S_{hh_m} S_{hh_s}^* \rangle & 0 & \langle S_{hh_m} S_{hh_s}^* \rangle - 4 \langle S_{hv_m} S_{hv_s}^* \rangle \\ 0 & 2 \langle S_{hv_m} S_{hv_s}^* \rangle & 0 \\ \langle S_{hh_m} S_{hh_s}^* \rangle - 4 \langle S_{hv_m} S_{hv_s}^* \rangle & 0 & \langle S_{hh_m} S_{hh_s}^* \rangle \end{bmatrix} \quad (24)$$

H_2 : $\log \tilde{\mathbf{S}}_{1,1} + \log |\tilde{\mathbf{S}}_{3,3}| + 3$, where

$$\hat{\mathbf{C}}_{\text{sym}} = \mathbf{U}^H \begin{bmatrix} \tilde{\mathbf{S}}_{1,1} & 0 \\ 0 & \tilde{\mathbf{S}}_{3,3} \end{bmatrix} \mathbf{U} \quad \text{and} \quad \tilde{\mathbf{S}} = \mathbf{U} \begin{bmatrix} \tilde{\mathbf{S}}_{1,1} & \tilde{\mathbf{S}}_{1,3} \\ \tilde{\mathbf{S}}_{3,1} & \tilde{\mathbf{S}}_{3,3} \end{bmatrix} \mathbf{U}^H.$$

H_3 : $\log |((1/2)(\tilde{\mathbf{S}}_{1,1} + \mathbf{J}\tilde{\mathbf{S}}_{1,1}^T \mathbf{J}))| + \log \tilde{\mathbf{S}}_{2,2} + 3 + \log 2$, where

$$\hat{\mathbf{C}}_{\text{sym}} = \boldsymbol{\Sigma}^H \boldsymbol{\nu}^H \begin{bmatrix} \frac{1}{2}(\tilde{\mathbf{S}}_{1,1} + \mathbf{J}\tilde{\mathbf{S}}_{1,1}^T \mathbf{J}) & 0 \\ 0 & \tilde{\mathbf{S}}_{2,2} \end{bmatrix} \boldsymbol{\nu} \boldsymbol{\Sigma}$$

and

$$\tilde{\mathbf{S}} = \boldsymbol{\nu} \boldsymbol{\Sigma} \boldsymbol{\Sigma}^H \boldsymbol{\nu}^H = \begin{bmatrix} \tilde{\mathbf{S}}_{1,1} & \tilde{\mathbf{S}}_{1,2} \\ \tilde{\mathbf{S}}_{2,1} & \tilde{\mathbf{S}}_{2,2} \end{bmatrix}.$$

H_4 : $\log(\tilde{\mathbf{S}}_{1,1}) + 2 \log((\tilde{\mathbf{S}}_{2,2} + \tilde{\mathbf{S}}_{3,3})/2) + 3 + \log 2$, $\hat{\mathbf{C}}_{\text{sym}} = \boldsymbol{\Sigma}^H \text{diag}(\tilde{\mathbf{S}}_{1,1}, ((\tilde{\mathbf{S}}_{2,2} + \tilde{\mathbf{S}}_{3,3})/2), ((\tilde{\mathbf{S}}_{2,2} + \tilde{\mathbf{S}}_{3,3})/2)) \boldsymbol{\Sigma}$, where $\tilde{\mathbf{S}} = \boldsymbol{\Sigma} \boldsymbol{\Sigma}^H$, and $\tilde{\mathbf{S}}_{1,1}$, $\tilde{\mathbf{S}}_{2,2}$, and $\tilde{\mathbf{S}}_{3,3}$ are its diagonals entries.

In order to overcome the multiple hypothesis testing problems, [9] considers a model order selector [i.e., Akaike' information criterion, Bayesian information criterion (BIC), generalized information criterion (GIC), and exponentially embedded family (EEF)] [22], and shows that BIC, GIC, and EEF are more reliable and provides a superior performance. For this reason, we consider herein the two last approaches for our tests, namely, the GIC approach [22] and the EEF approach [23], we believe that this guarantees sufficient accuracy. Their general theoretical formulations are described next.

1) *Generalized Information Criterion*:

$$-2 \log(f(R|\hat{\mathbf{C}}^{(n)})) + n\eta(n, N) \quad (30)$$

where $\hat{\mathbf{C}}^{(n)}$ is the ML estimate of \mathbf{C} for n parameters and η represents the penalty term [22], [24].

Thus, for each of the four aforementioned hypotheses, the decision statistic becomes as follows [9].

H_1 :

$$2N \log |\mathbf{S}| + 6N + 6N \log \pi + 9\eta.$$

H_2 :

$$2N \log |\tilde{\mathbf{S}}_{1,1}| + 2N \log |\tilde{\mathbf{S}}_{3,3}| + 6N \\ + 6N \log \pi + 5\eta.$$

H_3 :

$$2N \log \left| \left(\frac{(\tilde{\mathbf{S}}_{2,2} + \mathbf{J}\tilde{\mathbf{S}}_{2,2}^T \mathbf{J})}{2} \right) \right| + 2N \log \tilde{\mathbf{S}}_{1,1} \\ + 6N + 2N \log 2 + 6N \log \pi + 3\eta.$$

H_4 :

$$2N \log(\hat{\mathbf{S}}_{1,1}) + 4N \log \left(\frac{\hat{\mathbf{S}}_{2,2} + \hat{\mathbf{S}}_{3,3}}{2} \right) + 6N \\ + 2N \log(2) + 6N \log \pi + 2\eta.$$

2) *Exponentially Embedded Families*:

$$\text{EEF}(i) = \left\{ l_{G_i}(\vec{\mathbf{Z}}_{\text{obs}}) - n(i) \left[\log \left(\frac{l_{G_i}(\vec{\mathbf{Z}}_{\text{obs}})}{n(i)} \right) + 1 \right] \right\} \\ \times u \left(\frac{l_{G_i}(\vec{\mathbf{Z}}_{\text{obs}})}{n(i)} + 1 \right) \quad (31)$$

where

$$l_{G_i}(\vec{\mathbf{Z}}_{\text{obs}}) = 2 \log \left[\frac{f(\vec{\mathbf{Z}}_{\text{obs}}; \hat{\boldsymbol{\Omega}}_m^{(n(i))})}{f(\vec{\mathbf{Z}}_{\text{obs}}; \hat{\boldsymbol{\Omega}}_m^{(0)})} \right], \quad i = 1, 2, 3, 4$$

with $u(\cdot)$ the Heaviside step function, and for each of the four aforementioned hypotheses, $n(i)$ represents the associated number of unknown parameters and under the hypothesis that $\hat{\boldsymbol{\Omega}}_m^{(0)}$ is defined as n -dimensional identity matrix, i.e., $\hat{\boldsymbol{\Omega}}_m^{(0)} = \mathbf{I}_n$, $l_{G_i}(\vec{\mathbf{Z}}_{\text{obs}})$ becomes [9]

H_1 :

$$l_{G_1}(\vec{\mathbf{Z}}_{\text{obs}}) = -2N \log |\mathbf{S}| - 6N + 2\text{tr}(\mathbf{S}_0).$$

H_2 :

$$l_{G_2}(\vec{\mathbf{Z}}_{\text{obs}}) = -2N \log |\tilde{\mathbf{S}}_{1,1}| - 2N \log |\tilde{\mathbf{S}}_{3,3}| \\ - 6N + 2\text{tr}(\mathbf{S}_0).$$

H_3 :

$$l_{G_3}(\vec{\mathbf{Z}}_{\text{obs}}) = -2N \log(\tilde{\mathbf{S}}_{2,2}) \\ - 2N \log \left| \left(\frac{1}{2}(\tilde{\mathbf{S}}_{1,1} + \mathbf{J}\tilde{\mathbf{S}}_{1,1}^T \mathbf{J}) \right) \right| \\ - 6N - 2N \log(2) + 2\text{tr}(\mathbf{S}_0).$$

H_4 :

$$l_{G_4}(\vec{\mathbf{Z}}_{\text{obs}}) = -2N \log(\hat{\mathbf{S}}_{1,1}) - 2N \log \left(\frac{\hat{\mathbf{S}}_{2,2} + \hat{\mathbf{S}}_{3,3}^*}{2} \right) \\ - 2N \log \left(\frac{\hat{\mathbf{S}}_{2,2}^* + \hat{\mathbf{S}}_{3,3}}{2} \right) - 6N \\ - 2N \log(2) + 2\text{tr}(\mathbf{S}_0).$$

Here, we should mention that we can combine both approaches and make a joint decision which give more reliable decision. In the following, we use them separately.

A. Proposed Framework

Fig. 1 summarizes the overall pipeline of the proposed framework as four main steps. The input consists of a PolInSAR cross-covariance matrix data set (i.e., \mathbf{C}_{12} or \mathbf{C}_{21}). As the matrix exhibits a special form for each of symmetries, we use a particular transformation for each of the symmetries detection, and after performing matrices' transformations, we apply the model order selection using EEF/GIC for detecting the pertinent symmetry. Then, we use the interferometric information to retrieve the associated phase center for the i th resolution cell. The phase is estimated by isolating one polarization channel that scatters from the top of the canopy and, hence, generates a height estimate directly by

$$h_v = \frac{\arg(\gamma_{w_v}) - \hat{\phi}_g}{k_z} \quad (32)$$

where w_v is often taken to be HV, as this channel is dominated by volume scattering. However, the phase center of HV can be located anywhere between the top of the canopy and its foot. These depend on two parameters related to the vegetation, namely, the mean wave extinction and vertical canopy structure variation, as is the radar frequency which controls the penetration depth.

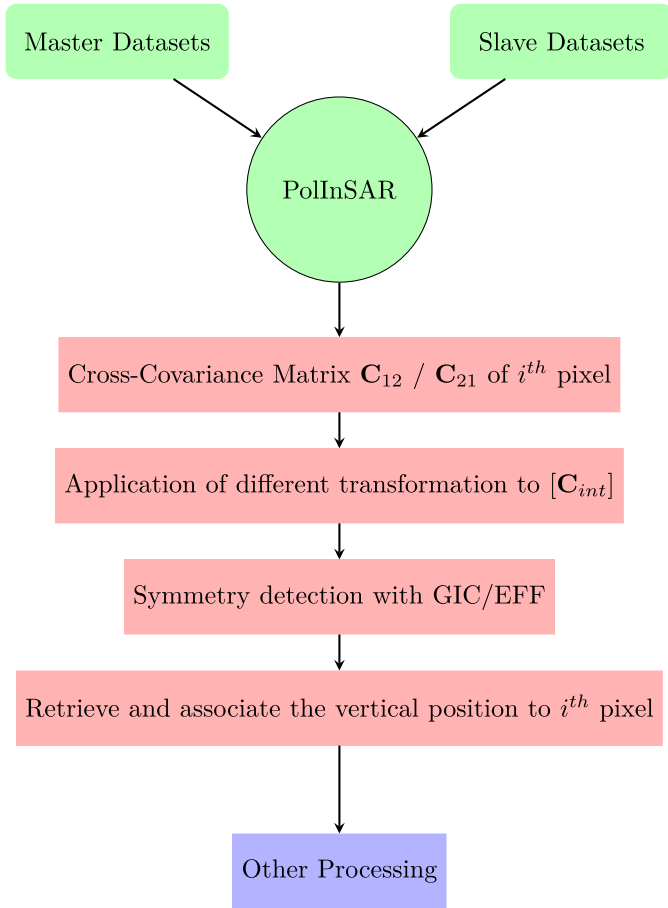


Fig. 1. Overall pipeline of PolInSAR covariance symmetries detection.

The estimated volume height corresponds to the phase center of the volume scattering mechanism and not the top of the trees. Consequently, the estimated height is greater than half of the actual tree height, but it is less than the full height [16]. Then, the inverse transformation is applied by assuming an ideal form of the matrix for each symmetry case, and thereafter, the H-A- α extraction is applied to the ideal form of the covariance matrix.

IV. PERFORMANCE ANALYSIS

In this section, the performance analysis and its validation are achieved first using simulated data through Monte Carlo simulations. The performance is also assessed using two real-L-band data sets. The height estimation of the detected symmetries is also assessed on real data.

A. Analysis Using Simulated Data

In spite that the cross-covariance matrix has different form comparing with the covariance matrix due to the interferometric information and temporal baseline bias, however, it still depicts the same form when encountering a symmetry case [7]. The best way to test the detection of symmetries within the cross-covariance matrix is through a series of Monte Carlo simulations [17]. For this aim, we generate some data samples

that fit the form of the theoretical cross covariance (i.e., \mathbf{C}_{12} and \mathbf{C}_{21}) in case of each of the four scenarios as follows.

1) *No Symmetry*: A random cross-covariance matrix is generated using Monte Carlo simulations.

2) *Reflection Symmetry*:

$$\begin{bmatrix} 1 & 0 & 0.4 - 0.25j \\ 0 & 0.25 & 0 \\ 0.4 + j0.25 & 0 & 0.4 \end{bmatrix} \times e^{j\varphi_{\text{int}}}. \quad (33)$$

3) *Rotation Symmetry*:

$$\begin{bmatrix} 1 & j0.25e^{j\varphi_{\text{hv}}} & 0.2 \\ -j0.25e^{j\varphi_{\text{hv}}} & 0.3 & j0.25e^{j\varphi_{\text{hv}}} \\ 0.2 & -j0.25e^{j\varphi_{\text{hv}}} & 1 \end{bmatrix} \times e^{j\varphi_{\text{int}}} \quad (34)$$

4) *Azimuth Symmetry*:

$$\begin{bmatrix} 1 & 0 & 0.6 \\ 0 & 0.2 & 0 \\ 0.6 & 0 & 1 \end{bmatrix} \times e^{j\varphi_{\text{int}}} \quad (35)$$

where φ_{int} represents the interferometric phase and is selected randomly within $[0, 2\pi]$, and φ_{hv} represents the phase shift between polarizations and is selected randomly within $[0, \pi]$.

Fig. 2 shows the proportion of a correct classification for $N = 25$ data vectors, relative to each of the four analyzed models. The subplots refer, respectively, to the four considered covariance scenarios, and the performance measures are related to three-order selectors (i.e., GIC with $\rho = 2$, GIC with $\rho = 3$, and EEF).

Results show that the EEF and GIC approaches provide a good performance except for the cases where symmetries lead to similar structures in the covariance matrix (i.e., azimuth and rotation symmetries), in which the probability of correct classification reaches about 95%, which is more than acceptable.

B. Analysis on Real Data

The performance analysis and its validation are assessed using two real data sets. First, we have used the fully polarimetric L-band (1.3 GHz) Oberpfaffenhofen E-SAR repeat pass data set, with an incidence angle ranging between 27° and 55° . The site contains different regions with various properties (Fig. 3), namely, urban areas, such as that surrounded by a red rectangle, forested area surrounded by a green rectangle, and bare areas that contain an aircraft runway referred to in the figure by a yellow arrow. Moreover, for reasons of acquisition parameters availability and flexibility, such as frequency, wavenumber, baseline, and flat earth, necessary elements for height retrieval, we have also used the BiosSAR-II fully polarimetric L-band data set, wherein we can associate symmetries to its vertical position. Precisely, an area of 600×3000 pixels has been selected for the test. Almost all the parts of the zone are forested and situated in the province of Västerbotten in northern Sweden [see Fig. 6(a)].

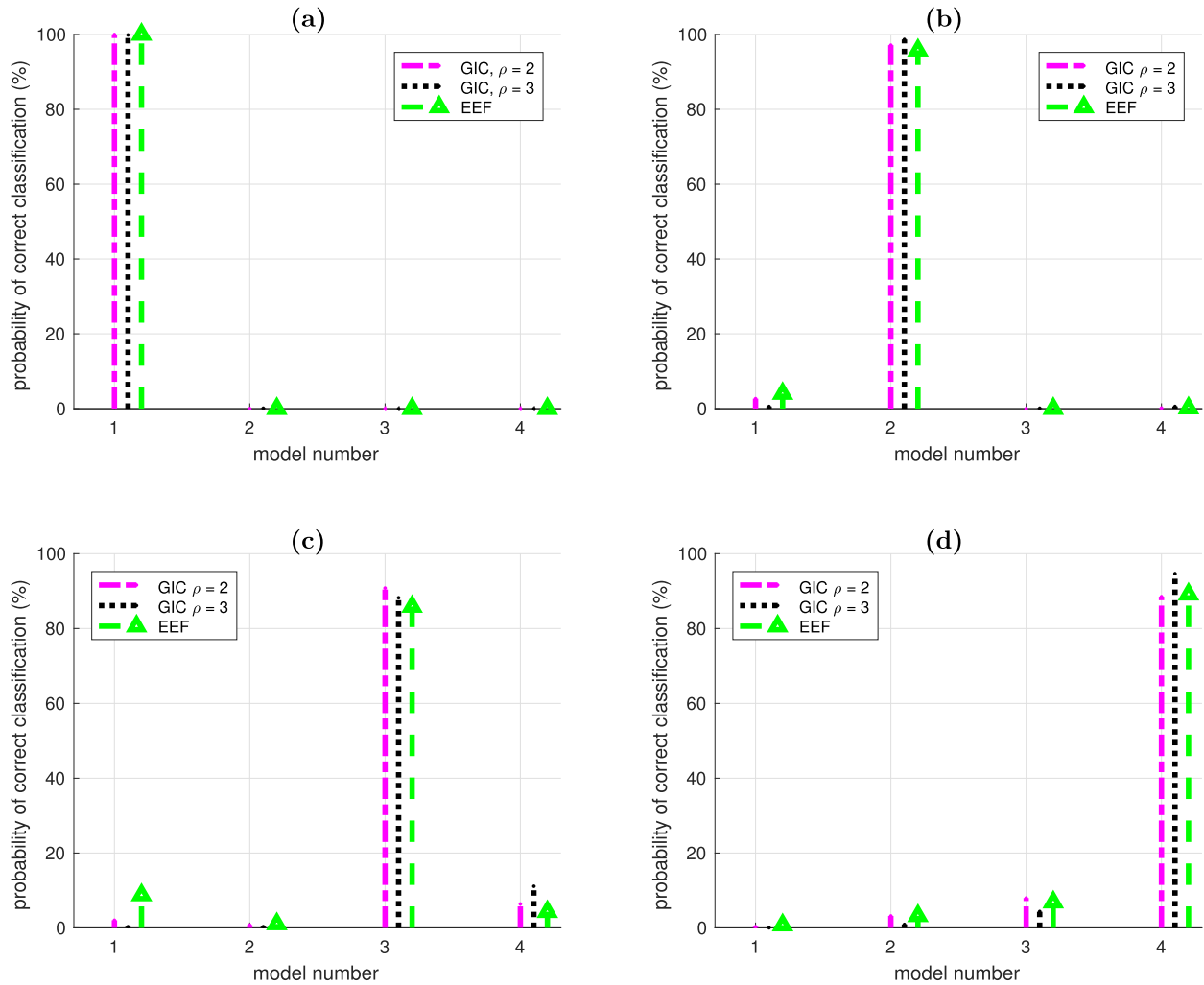


Fig. 2. Probability of correct classification for $N = 25$ data vectors. (a) Random cross-covariance matrix. (b) Reflection cross-covariance matrix form. (c) Rotation cross-covariance matrix form. (d) Azimuth cross-covariance matrix form. H_1 : no symmetry detected with black. H_2 : reflection symmetry detected with blue. H_3 : rotation symmetry detected with red. H_4 : azimuth symmetry detected with green.

1) *General Test Using GIC and EEF*: As mentioned earlier, scatterers with specific geometric properties exhibit a specific symmetry. For instance, in red rectangle in Fig. 3(b), one can clearly notice the urban area manifests reflection (blue) and no symmetry (black). This is due to the fact that the urban areas contain, in general, a large amount of anisotropic scattering provided from man-made structures, which mean a nonnull degree of correlation between copolarization and cross-polarization channels [25]. This fact is manifested in the absence of both the reflection and azimuth symmetries. This is noticed clearly on the fencing of the neighboring agricultural land, indicated by the red arrow in Fig. 3(b), Notice that for the same fencing but oriented differently exhibits rotation symmetry (indicated by a white arrow).

On the other hand, the reflection symmetry implies a null correlation between copolarization and cross-polarization channels [25], which can be produced for soil surfaces without row structures [blue rectangle in Fig. 3(a)]. It is also the case for volume scattering from random layer media containing spherical particles [26] at standard frequencies (C- or L-band),

this property is usually used for polarimetric calibration [27]. A randomly perturbed periodic rough surface obeys the constraints imposed by reflection symmetry [5]. This supports the distribution of blue in Fig. 3(b), which is in general an agriculture field. The azimuthal symmetry possesses the characteristics of both the reflection and rotation symmetries, which means that the reflection symmetry is guaranteed in any vertical plane passing the axis of rotation [25], the azimuth symmetry is shown by a uniformly random medium with spherical scatterers [7], usually, the forest canopy is an example for such case (even at penetrating frequencies), and can also be exhibited by slightly rough surfaces at low incidences [28], [29]. In Fig. 3(b), we notice that the green that represents the azimuth reflection appears mostly in the forested areas (yellow rectangle). However, the azimuth symmetry must be interspersed with underlying ground reflection symmetry, more or less pursuant to the *in situ* pattern. It can be clearly observed the important difference between classes distinction by comparing Fig. 3(b) (PolInSAR detection) and Fig. 4 (PolSAR detection). In particular, comparing the reflection and

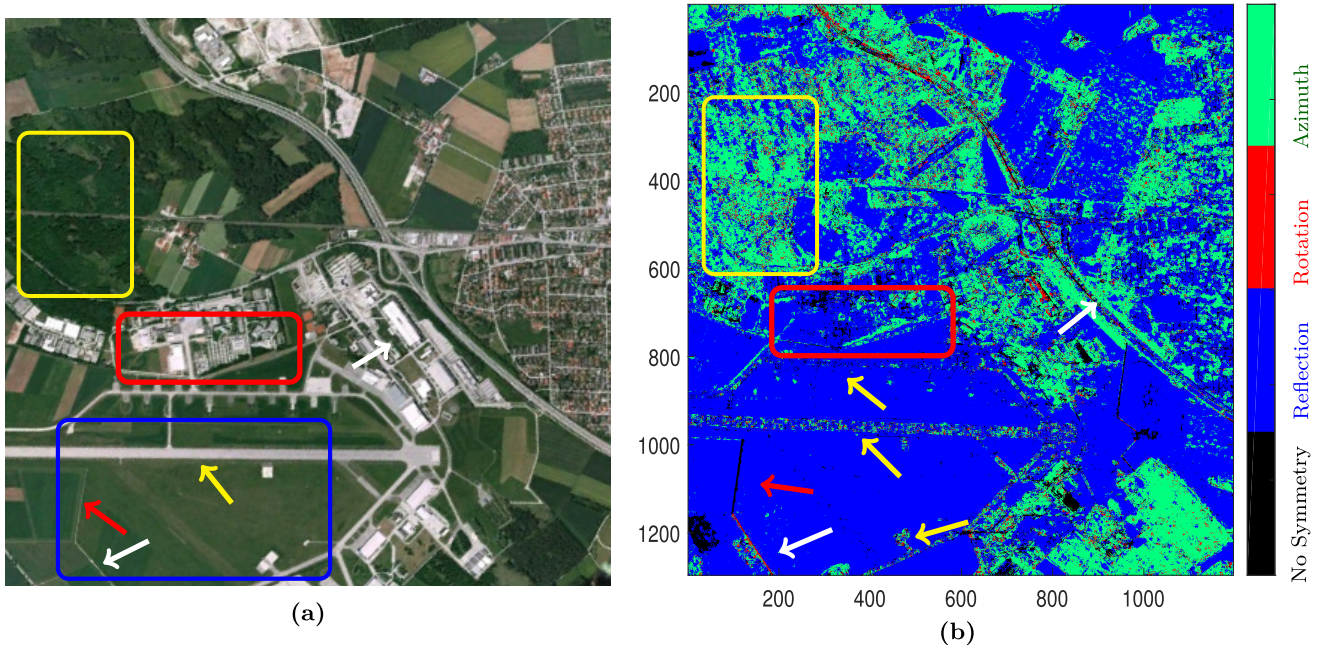


Fig. 3. (a) Optical image of the test site in Oberpfaffenhofen (Google Earth). (b) GIC index associated with the four hypotheses performed using a cross covariance matrix. H_1 : no symmetry with black. H_2 : reflection symmetry with blue. H_3 : rotation symmetry with red. H_4 : azimuth symmetry with green.

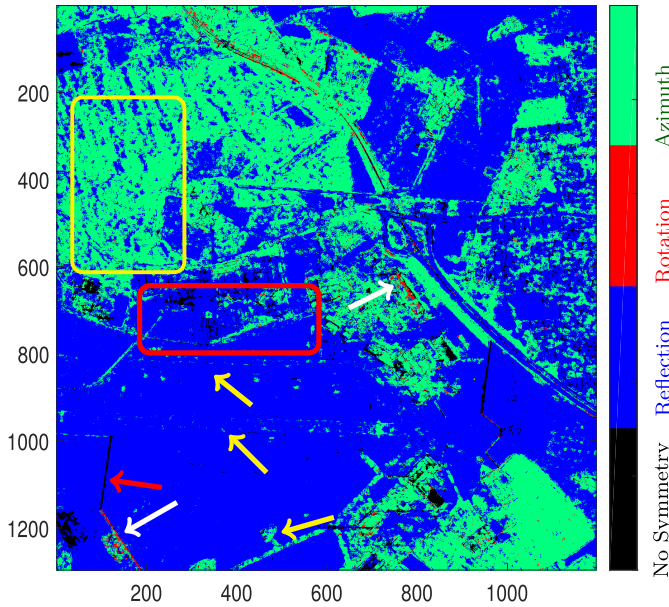


Fig. 4. GIC index associated with the four hypotheses performed using polarimetric covariance matrix. H_1 : no symmetry with black. H_2 : reflection symmetry with blue. H_3 : rotation symmetry with red. H_4 : azimuth symmetry with green.

azimuth symmetries in forested areas, polarimetric detection seems to confuse trees canopy with gaps between trees, which is reflected by the lack of reflection symmetry in those areas. It can also be noticed that some patterns are missed as well as lot of symmetries in comparison with the PolInSAR detection [see yellow arrows in Figs. 3(b) and 4]; for example, the aircraft runway has disappeared completely and confused with the nearby field, as well as the rotation symmetry which has greatly decreased particularly in the forested area.

Algorithm 1 H-A- α Decomposition Using Symmetry

```

initialization ;
while not at end of the dataset do
  Data:
  1) read current pixel ;
   $C_{int} = \begin{pmatrix} \langle S_{hh_m} S_{hh_s}^* \rangle & \sqrt{2} \langle S_{hh_m} S_{hv_s}^* \rangle & \langle S_{hh_m} S_{vv_s}^* \rangle \\ \sqrt{2} \langle S_{hv_m} S_{hh_s}^* \rangle & 2 \langle S_{hv_m} S_{hv_s}^* \rangle & \sqrt{2} \langle S_{hv_m} S_{vv_s}^* \rangle \\ \langle S_{vv_m} S_{hh_s}^* \rangle & \sqrt{2} \langle S_{vv_m} S_{hv_s}^* \rangle & \langle S_{vv_m} S_{vv_s}^* \rangle \end{pmatrix}$ 
  ;
  2) Perform transformations and compute the matrices  $S, \tilde{S}, \tilde{\tilde{S}}$ , and  $\tilde{\tilde{S}}$  ;
  3) Estimate dominant symmetry using GIC/EEF of the pixel, as described in Section III ;
  4) Perform the inverse transformation of the pixel matrix, and get the canonic form of the cross-covariance matrix by eliminating noise ;
  5) Extract H-A- $\alpha$  decomposition starting from the new matrix form ;
end
Result: 2D H-A- $\alpha$  decomposition map.

```

2) *H-A- α Decomposition Using Symmetries*: The knowledge of the symmetry is very important of many PolSAR/PolInSAR applications. In order to give an additional evidence of the effectiveness of the approach, we have used H-A- α decomposition with and without using the symmetry information in order to highlight its contribution. Algorithm 1 shows all the basic steps for the H-A- α decomposition using a symmetry for each pixel of the image. And for more details about the procedure, see [9].

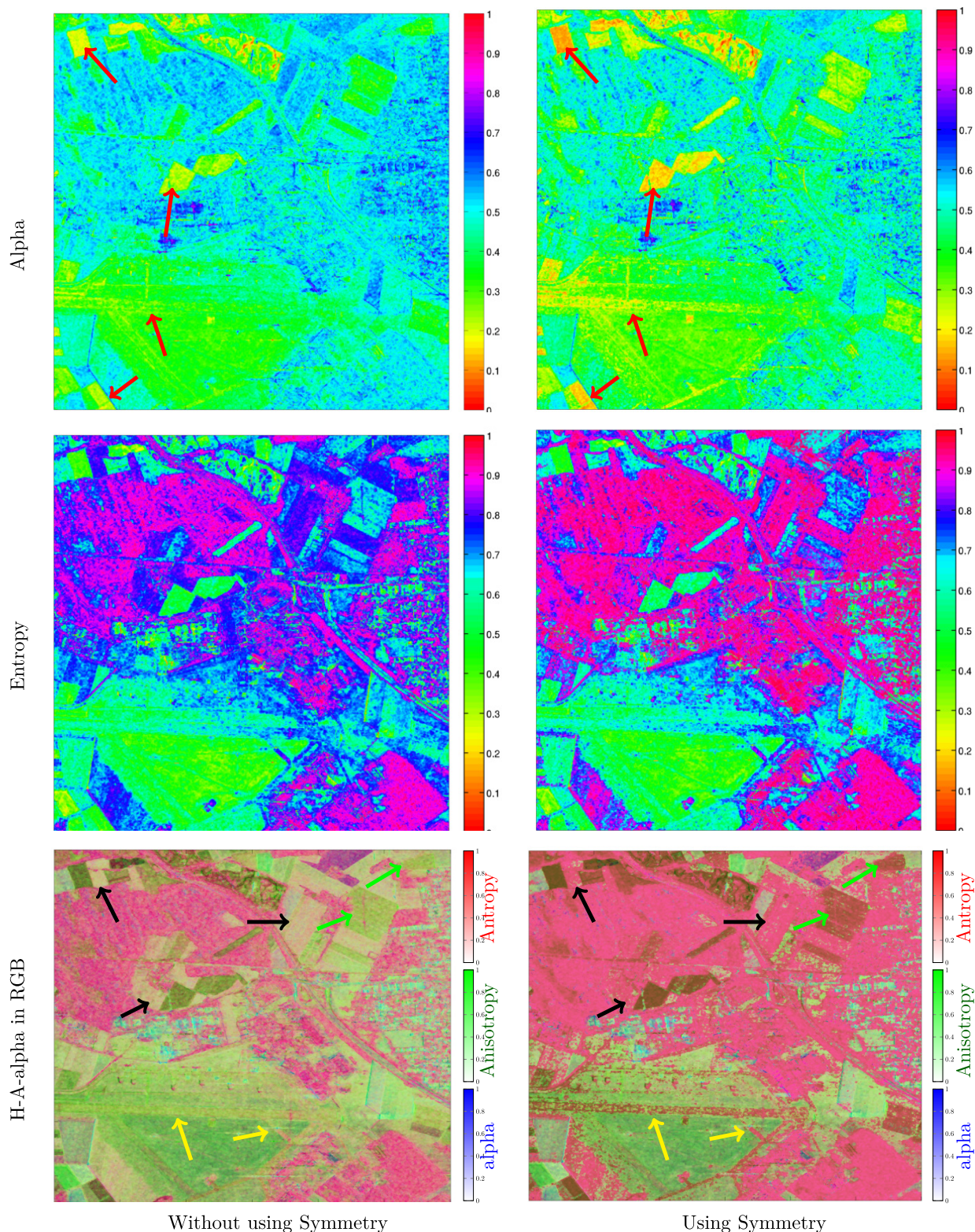


Fig. 5. Comparison between, alpha “ α ,” entropy “H,” and RGB of H-A- α using symmetry properties and without (Left column contains the H-A- α performed without using symmetries, and right column performed using symmetries).

In Fig. 5, α and H matrices are plotted with/without using the symmetries information. We have used GIC (with $\rho = 3$, and 3×3 sliding window). From Fig. 5, we can notice that some areas appear clearer on the right side image than that of

the left side one (red arrows), such as the aircraft landing runway, which appears well delineate. This is manifested clearly in the RGB image in the bottom of Fig. 5. As is known [10], the parameter α is associated with the nature of

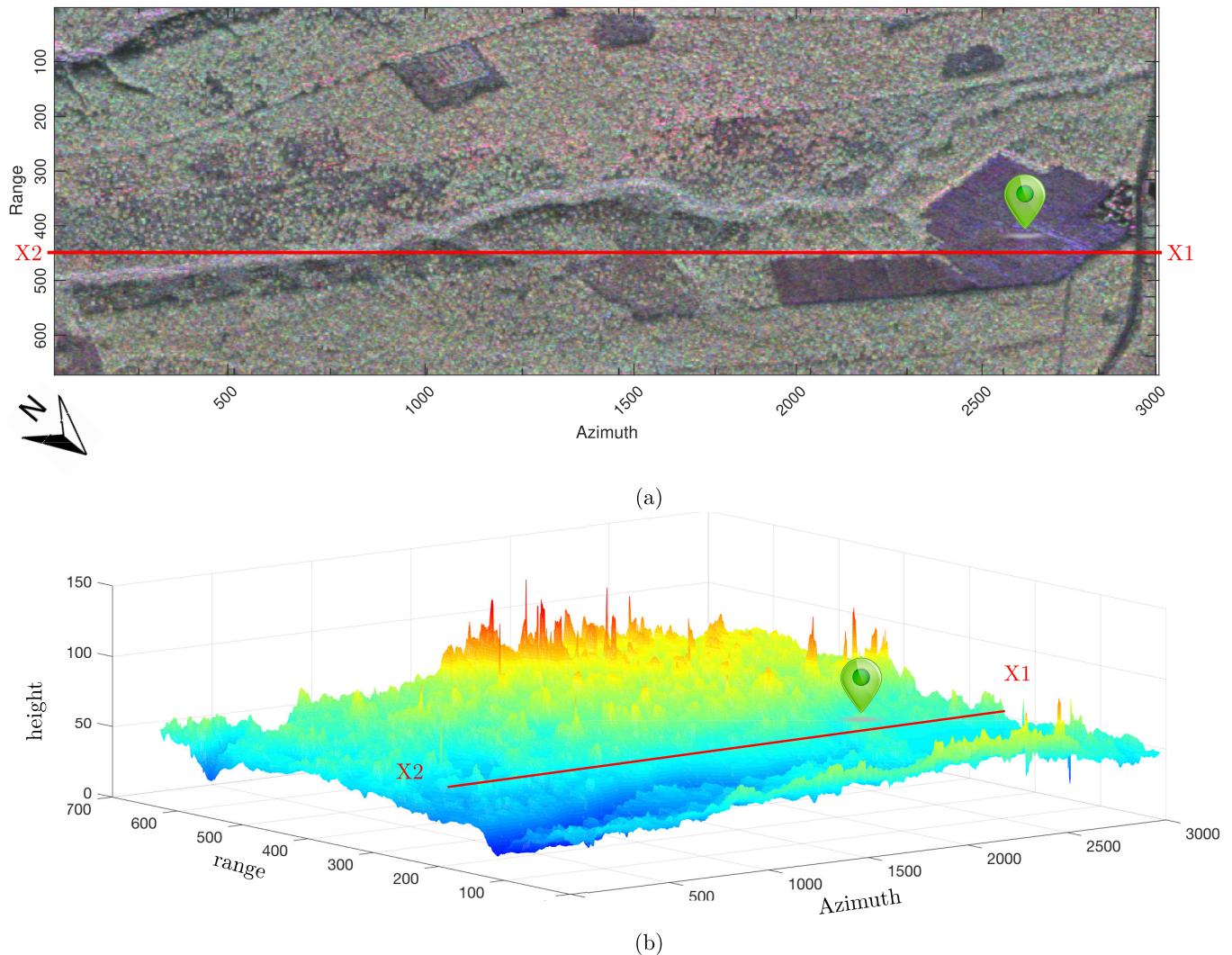


Fig. 6. (a) Pauli-RGB coded image of the selected region (red: HH-VV, green: 2HV, and blue: HH+VV) from the BiosAR-II data set; the region is located at $64^{\circ}14'2.72''$ N latitude and $19^{\circ}47'52.47''$ E longitude (location indicated by green map marker). (b) 3-D phase difference map of the selected region of test with the surface phases contour plot on the plane. The red line indicates the row chosen as an example for phase profile with symmetries.

the scattering mechanism. If α is zero, then the mechanism is that of a canonical surface scattering. This translated the appearance of the airplane track. In the other extreme case, i.e., $\alpha = 90^{\circ}$, the backscattering mechanism is that of a dihedral or helices. It is known [10] that the entropy of the target is defined as the randomness indicator of the global scattering phenomenon. A zero entropy indicates that the observed target is pure and the scattering is deterministic [10], while the completely random character of the observed target is defined by an entropy equal to one. The test site consists mainly of forest or agricultural areas, and the vegetation is characterized by randomness. Consequently, most regions reach a one $H \cong 1$, and this appears more readable on the entropy made using the symmetry (right images). To give an additional evidence of the effectiveness of the approach, we have represented the H-A- α decomposition in RGB colors, and the results do not need scrupulous attention to see the difference. For example, the aircraft track (yellow arrow in the bottom right of Fig. 5) appears as a different class compared

with the neighboring flat area in contrast to the left RGB image [Fig. 5 (bottom left)]. In addition, we notice the emergence of new areas in the forested region indicated by the red arrows [Fig. 5 (top right) and Fig. 5 (bottom) by green arrows], which are in fact a bare soil. In addition, we notice that some regions with medium-length vegetation (indicated by black arrows) are assigned to the same class as forested.

3) *Vertical Position of Symmetries*: Based on the fact that each of the symmetries is related to one or other form of scattering geometry [5], [7], symmetries' map can be used as the preland/postland classifier. It has also the potential to provide number of benefits To PolInSAR applications. Thus, producing a 3-D symmetries map instead of a 2-D map can be very convenient and promising. In this section, we attempted to validate the processing algorithm by associating vertical position. To this aim, we have used BioSAR II campaign data set, which offers users the capability to choose between a variety of baseline with k_z values between 0.01 and 0.3 rad/m

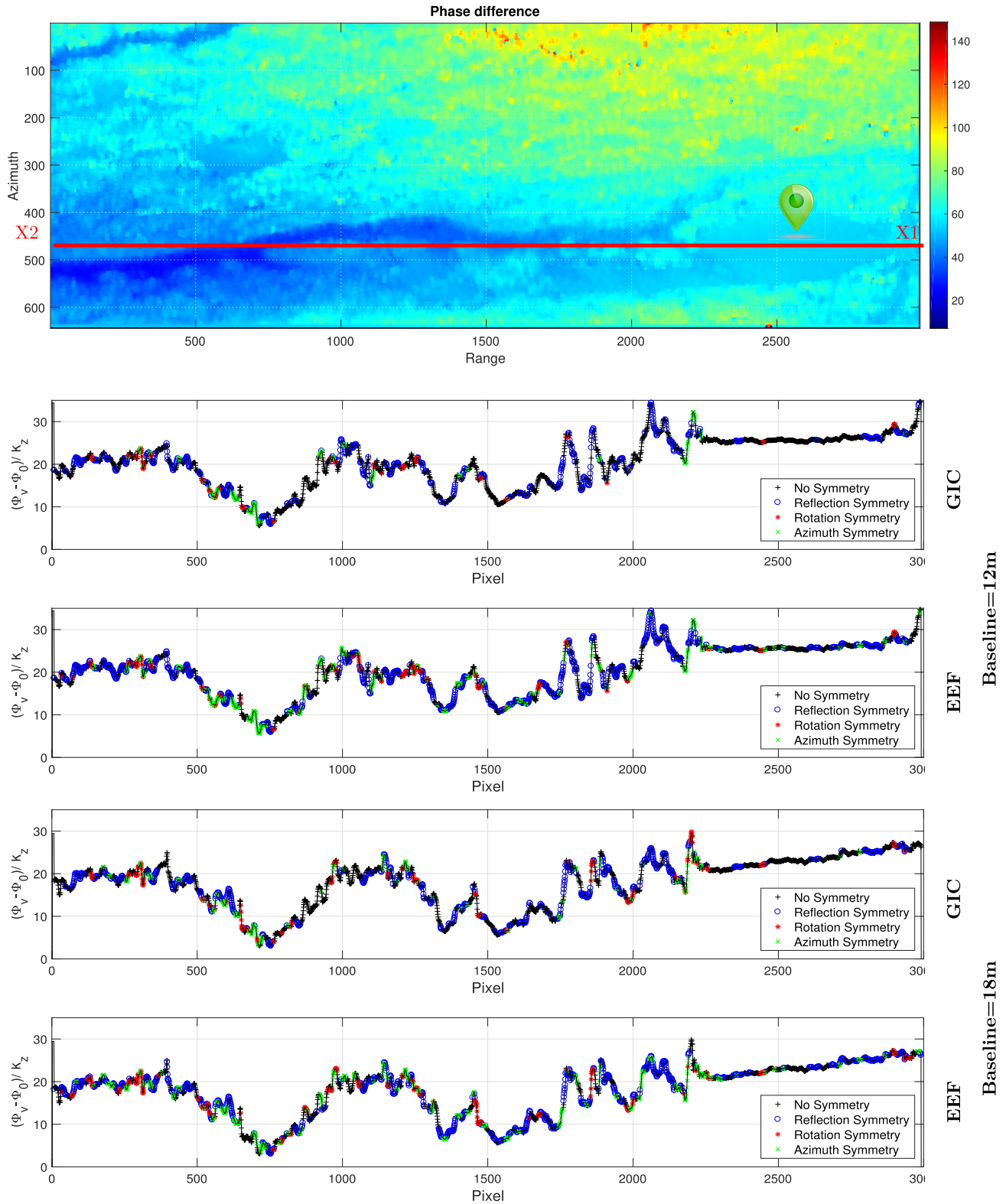


Fig. 7. (Top) Phase difference images of the test site performed using the formula (32). The four graphs correspond to the estimated horizontal phase profile associated with detected symmetries according to GIC and EEF (black: no symmetries, blue: reflection symmetries, red: rotation symmetries, and green: azimuth symmetries) carried out along the red line in Fig. 6. The two graphs on bottom correspond to an 18-m baseline, and the two other correspond to a 12-m baseline.

over a vast forested area with a variety of trees species. The BioSAR II data set is acquired at L-band over Krycklan forest site and came with a related ground truth, such as

trees species and height, digital elevation model (DEM), and stand density helpful for cross validation. The mean forest height in Krycklan is of 18 m and the mean biomass level

is of 90 t/ha. The measured maximum forest height is about 30 m. The topography in the site is characterized by moderate slopes and a height variation. The objective is to use the cross-covariance matrix to detect symmetries and its related height by using DEM differencing. Fig. 6 shows the Pauli-RGB coded (i.e., red: HH–VV, green: 2HV, and blue: HH+VV) image of the selected region, where the horizontal red line denotes the phase profile transaction, which passes through homogeneous forest, groove, and an agriculture region.

For a better visual comparison, Fig. 7 shows all detected symmetries by different estimators according to GIC and EEF (black: no symmetries, blue: reflection symmetries, red: rotation symmetries, and green: azimuth symmetries), as well as their vertical positions performed using formula (32) from two different baselines, namely, 12 m (graphs on top) and 18 m (graphs on bottom) carried out along the red line. Only the PolInSAR phase difference map, scaled from 0 to 120 m, from 12-m baseline is superimposed on the top (Fig. 7). The maximum phase difference obtained with the two considered baselines is 138 m for 12-m baseline and 133 m for 18-m baseline.

As shown in Fig. 7, the detected symmetries are approximately the same for the two baselines more resemblance for the same detectors. Moreover, it can be observed that the difference appears mainly between the reflection and azimuth symmetries. This is caused by two main reasons: 1) the similarity between the two covariance matrices (azimuth and rotational symmetries) which disturbs the decision and 2) the difference in the angle of view between the two baselines which causes a change in the reflection geometry.

V. CONCLUSION

In this paper, we have extended a recent framework for detecting covariance symmetries to the PolInSAR data; the formulation of detecting covariance symmetries within the PolSAR data has been adapted to PolInSAR in order to detect not only the symmetry but also its associated interferometric information, by using the cross-covariance matrix instead of the cocovariance (namely, master or slave). The validation of the algorithm has been achieved using the E-SAR repeat pass PolInSAR data acquired at L-band over the Oberpfaffenhofen area in Germany. The procedure considers the GIC approach in order to deal with the multiple hypothesis testing problem (i.e., no symmetry, reflection symmetry, rotation symmetry, and azimuth symmetry), since that GIC provides good results. The fact that makes this approach more reliable is the coherent distribution of the index of symmetry, which corresponds to the theory and conforms to the ground reality, for example, the azimuth symmetry in the forested area and the reflection in surfaces.

The results were very encouraging and satisfactory and have opened a promising field of future applications, for example, it might be exploited to separate some elements over the forested areas in order to increase the accuracy of inversion methods. Moreover, it must pay attention to the promising benefits that could be drawn from PolInSAR symmetry detection, and the added value in the PolInSAR data

retrieval applications, where it can be used as a criterion to confirm the validity of the vegetation height retrieval process. For example, in the RVoG model [29], the inversion method is based on least squares line fit to find the best fit straight line inside the unit circle. And the far intersection with a unit circle to HV coherence represents the ground topography, while the height is assumed to be represented by the HV polarization. The use of symmetry, in this case, would increase the reliability of the inversion by taking it as an additional assumption, as the reflection symmetry is related mostly to the vegetation, and the azimuth symmetry can reveal about ground surfaces. Future works will be devoted to the use of this procedure for pure PolInSAR applications.

ACKNOWLEDGMENT

The authors would like to thank European Space Agency (ESA), the BioSAR Team from ESA, and the German Aerospace Center (DLR), for the data provision and for the science support.

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