

# Exploring and Mitigating Gender Bias in Book Recommender Systems with Explicit Feedback

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## Research Article

**Keywords:** Recommender System, Gender Bias, Fairness

**Posted Date:** July 28th, 2022

**DOI:** <https://doi.org/10.21203/rs.3.rs-1876910/v1>

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# Exploring and Mitigating Gender Bias in Book Recommender Systems with Explicit Feedback

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## Abstract

Recommender systems are indispensable because they influence our day-to-day behavior and decisions by giving us personalized suggestions. Services like Kindle, Youtube, and Netflix depend heavily on the performance of their recommender systems to ensure that their users have a good experience and to increase revenues. Despite their popularity, it has been shown that recommender systems reproduce and amplify the bias present in the real world. The resulting feedback creates a self-perpetuating loop that deteriorates the user experience and results in homogenizing recommendations over time. Further, biased recommendations can also reinforce stereotypes based on gender or ethnicity, thus reinforcing the filter bubbles that we live in. In this paper, we address the problem of gender bias in recommender systems with explicit feedback. We propose a model to quantify the gender bias present in book rating datasets and in the recommendations produced by the recommender systems. Our main contribution is to provide a principled approach to mitigate the bias being produced in the recommendations. We theoretically show that the proposed approach provides unbiased recommendations despite biased data. Through empirical evaluation on publicly available book rating datasets, we further show that the proposed model can significantly reduce bias without significant impact on accuracy. Our method is model agnostic and can be applied to any recommender system. To demonstrate the performance of our model, we present the results on four recommender algorithms, two from the K-nearest neighbors family, UserKNN and ItemKNN, and the other two from the matrix factorization family, Alternating least square

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047 and Singular value decomposition. The extensive simulations on various  
048 recommender algorithms show the generality of the proposed approach.

049 **Keywords:** Recommender System, Gender Bias, Fairness  
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## 051 052 053 1 Introduction

054  
055 Recommender systems influence a significant portion of our digital activity.  
056 They are responsible for keeping the user experience afresh by recommending  
057 varied items from a catalog of millions of items and also adapt their recommen-  
058 dations according to the personality and taste of the user. Therefore, a sound  
059 recommender system may go a long way in improving user experience quality,  
060 hence the user retentivity of a digital outlet.  
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062 Recommender systems have historically been judged on their accuracy  
063 (Herlocker et al, 2004; Shani and Gunawardana, 2011). When it is concerned  
064 with other factors such as novelty, user satisfaction, and diversity (Hurley and  
065 Zhang, 2011; Ziegler et al, 2005a; Knijnenburg et al, 2012), the focus continues  
066 to be just on the satisfaction of the information needs of the users. Although  
067 of immense importance to the relevance of a recommender system, these  
068 criteria do not capture the complete picture. In recent years, the public and  
069 academic community have scrutinized artificial intelligence systems regarding  
070 their fairness. It has been observed that the results generated by various  
071 recommender systems reflect the social biases that exist in human stratum  
072 (Ekstrand et al, 2018; Shakespeare et al, 2020; Boratto et al, 2019). Scholars  
073 have focused on identifying, quantifying, and mitigating the bias present in  
074 the results generated by recommendation systems. Burke (2017) presents a  
075 taxonomy of classes for fair recommendation systems. The author suggests  
076 different recommendation settings with fairness requirements such as fairness  
077 for only users, fairness for only items, and fairness for both users and items.  
078 Our work falls into fairness for only items category where bias is shown by a  
079 particular set of users against a specific set of items in the dataset. In particular,  
080 we are interested in studying and eliminating users' biasedness against the  
081 items associated with a specific gender in recommendation systems.

082 Bias prevention approaches can be classified according to the phase of the  
083 data mining process in which they operate: pre-processing, in-processing, and  
084 post-processing methods. Pre-processing methods aim to control distortion  
085 of the training set. In particular, they transform the training dataset so that  
086 the discriminatory biases contained in the dataset are smoothed, hampering  
087 the mining of unfair decision models from the transformed data. In-processing  
088 methods modify recommendation algorithms such that the resulting models do  
089 not entail unfair decisions by introducing a fairness constraint in the optimiza-  
090 tion problem. Lastly, post-processing methods act on the extracted data mining  
091 model results instead of the training data or algorithm. The method presented  
092 in our work is a hybrid of a pre-processing phase and a post-processing phase.

Two prominent studies have focused on gender bias in recommender systems. The work by Shakespeare et al (2020) establishes the existence of bias in the results of the music recommender systems, and the work by Ekstrand et al (2018) focuses on bias shown by Collaborative Filtering (CF) algorithms while recommending books written by women authors. Both the studies establish that the CF algorithms produced biased results after being fed the biased data from various socio-cultural factors. While both the works focus just on showing the existence of bias in the presence of the users' implicit feedback, we also consider the explicit feedback ratings and the bias that may arise out of it. Thus, our model handles the case when the items associated with specific gender might have received worse feedback than they otherwise ought to achieve by a set of users. We go one step further and propose a model to mitigate these biases by quantifying a particular user's bias and debiasing his or her feedback ratings. We theoretically show that the debiased ratings are unbiased estimators of the true preference of the user. Once the ratings are debiased, they are fed into the recommender algorithms as input to produce recommendations for the desired set of users. Since the recommender system is now fed with the debiased ratings, the resulting recommendations are free from the bias factor and avoid a self-perpetuating loop in the future.

The bias of an individual user reflects his or her taste. However, the KNN based algorithms produce recommendations based on similar characteristics between a set of users and naive implementation of these algorithms reflects the bias of one user in the recommendations produced for the other user. While not directly comparing the rating history of different users or items, Matrix Factorization algorithms rely on deriving latent factors, which depend on the rating history. Both the approaches make the system increasingly biased and homogenized after users interact with their biased recommendations and generate data for the next iteration. The above discussion suggests that though it is necessary to reflect the user's preference in the recommendations produced for him or her to achieve accuracy, it is equally necessary to prevent the bias of one user from reflecting in the recommendations of another similar user. Our research focuses on this particular objective.

Our debiased ratings assure that the biases of one user do not affect other users; however, it may lead to loss of accuracy because of not reflecting the user's own preferences. We introduce a new step called preference correction which injects the user's preference parameter into his/her own debiased recommendation to maintain the accuracy of the system. The novelty of our work lies in computing the user's preference parameter which not only helps in debiasing the ratings but also in maintaining the preferences of users. On the publicly available Book-Crossing dataset (Ziegler et al, 2005b) and Amazon Book Review dataset (Ni et al, 2019), we empirically show that this approach retained the significant reduction in bias and had minimal effect on the accuracy of the system. The bias reflected in the recommendations produced by the UserKNN, ItemKNN, ALS, and SVD algorithms is reduced by as much as 42.39%, 37.65%, 26.51%, and 41.43% respectively for the Amazon dataset

139 and by 37.82%, 30.73%, 24.99%, and 32.34% for the Book-Crossing dataset.  
140 When measured with respect to Root Mean Squared Error(RMSE), the final  
141 accuracy loss in the case of the Amazon dataset comes out to be 7.8%, 11.96%,  
142 12.49%, and 10.38% respectively for the four algorithms. In the case of the Book-  
143 Crossing dataset, the RMSE loss comes out to be 13.86%, 18.13%, 11.41%, and  
144 12.89% respectively. In particular, the following are our main contributions.

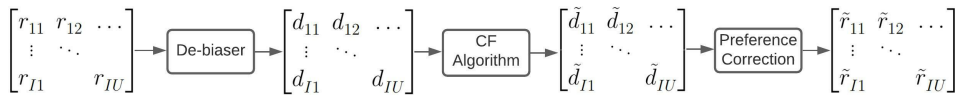
## 145 1.1 Contributions

- 146 • We propose a model to quantify the gender bias in the recommender  
147 system when explicit feedback is present.
- 148 • We propose a principled approach to debias the ratings given and theoret-  
149 ically show that the debiased ratings represent the unbiased estimator of  
150 the true preference of the user.
- 151 • We empirically evaluate our model on publicly available book datasets  
152 and show that the approach significantly reduced the biasedness in the  
153 system. To show the generality of our proposed approach, we show the  
154 results on four algorithms, UserKNN, ItemKNN, ALS, and SVD.
- 155 • In order to further enhance the accuracy of the debiased system, we  
156 propose an approach of preference correction that respects the user's own  
157 preferences towards his/her recommendations. We show that the final  
158 recommender system significantly reduces the bias in the system while  
159 not deteriorating the accuracy much.

## 162 2 Related Works

163 The problem of gender bias and discrimination has received lots of attention in  
164 recent works (Hajian et al, 2016). Many proposals like Pedreschi et al (2008),  
165 Pedreschi et al (2009), Ruggieri et al (2010), Thanh et al (2011), Manchuhan and  
166 Clifton (2014), Ruggieri et al (2014) are dedicated to detecting and measuring  
167 the existing biases in the datasets while other efforts (Kamiran et al, 2010, 2012;  
168 Hajian and Domingo-Ferrer, 2013; Hajian et al, 2014a,b; Dwork et al, 2011;  
169 Zemel et al, 2013) are focused on ensuring that data mining models do not  
170 produce discriminatory results even though the input data may be biased. Most  
171 of these works focus on the classical problem of classification. Amatriain et al  
172 (2011) discuss the application of various classification methods like Support  
173 Vector Machines, Artificial Neural Networks, Bayesian classifiers, and decision  
174 trees in recommender systems. Their findings indicated that a more complex  
175 classifier need not give a better performance for recommender systems, and  
176 more exploration is needed in this direction.

177 When considering "fairness for only users" according to the taxonomy  
178 presented by Burke (2017), Boratto et al (2019) and Tsintzou et al (2018)  
179 discuss the bias with respect to the preferential recommending of certain items  
180 only to the users of a specific gender. While weighted regularization matrix  
181 factorization studied in Boratto et al (2019) is only appropriate for implicit  
182 feedback, the Group Utility Loss Minimization proposed in Tsintzou et al (2018)  
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**Fig. 1:** Model schematics

works only with respect to the UserKNN algorithm. Both the papers address the issue of gender bias by employing post-processing algorithms that work only in limited settings. Though [Boratto et al \(2019\)](#) and [Tsintzou et al \(2018\)](#) have addressed the issue of fairness of recommender systems with respect to gender, they have done so from the perspective of recommending certain items only to the users of a specific gender. The difference between their work and our study lies in the fact that we focus on the more direct issue of gender bias in recommendations shown to items associated with a specific gender.

[Shakespeare et al \(2020\)](#) in their research highlight the artist gender bias in music recommendations produced by Collaborative Filtering algorithms. The work traces the causes of disparity to variations in input gender distributions and user-item preferences, highlighting the effect such configurations can have on user's gender bias after recommendation generation. [Mansoury et al \(2020\)](#) discuss the biases from the perspective of a specific group of individuals (for example, a particular gender) receiving less calibrated and hence unfair recommendations. [Ekstrand et al \(2018\)](#) explores the gender bias present in the book rating dataset. Our work is different from the works by [Shakespeare et al \(2020\)](#), [Mansoury et al \(2020\)](#) and [Ekstrand et al \(2018\)](#) in primarily two factors: (i) we consider explicit feedback as opposed to the implicit feedback, and (ii) we propose a principled approach to debias the ratings and theoretically show that the debiased ratings are unbiased estimators of true ratings.

The research by [Leavy et al \(2020\)](#) focuses on algorithmic gender bias and proposes a framework whereby language-based data may be systematically evaluated to assess levels of gender bias prevalent in training data for machine learning systems. Our work is different from this study as this study is focused on evaluating gender bias in the language and textual data settings, while ours deals with gender bias in a more traditional user-item rating setting.

A couple of works in fair recommender systems focus on improving the exposure of the items belonging to minority groups. They do so by upsampling the items associated with minority groups ([Boratto et al, 2021](#)), or by adding more data points to the dataset so as to achieve overall fairness ([Rastegarpanah et al, 2019](#)). On the contrary, our goal in this paper is to provide a systematic way to reduce the bias of one user affecting the recommendations to users. We do so via feeding unbiased ratings of the users to the recommender system. This direction avoids the self-perpetuating loop in the recommender system. Once such a system is deployed, there is no further need for interference by the system to ensure fairness. Further, no existing approaches provide a theoretical framework to mitigate the gender bias from the recommender system. We

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231 believe this is a strong first step in a new direction for a fair recommender  
 232 system.

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### 234 3 The Model

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236 Consider a recommender system having  $\mathcal{U} = \{1, 2, \dots, U\}$  users and  $\mathcal{I} =$   
 237  $\{1, 2, \dots, I\}$  items. Let  $\mathbb{D}$  and  $\mathbb{A}$  denote the set of items associated with disad-  
 238 vantaged group and advantaged group, respectively. For example, in a book  
 239 recommender system, the books represent the items;  $\mathbb{D}$  and  $\mathbb{A}$  represent the  
 240 set of books written by women and men authors respectively. With respect to  
 241 book recommender system, researchers have already shown that the data is  
 242 biased against female authors' books (Ekstrand et al, 2018).

243 Let  $r_{ui} \in [1, R]$  denote the rating that user  $u$  has given to the item  $i$ . As  
 244 opposed to previous works, we consider explicit feedback wherein biases may  
 245 not only arise from not giving the rating to the item but may also come from  
 246 giving a bad rating to the item. The user profile  $p_u = \{X_u, R_u\}$  represents the  
 247 set of books ( $X_u$ ) and the ratings ( $R_u = \{r_{ui}\}_{i \in X_u}$ ) that user  $u$  has given to  
 248 those items.

249 The proposed recommender system first pre-processes the data that: 1) finds  
 250 the log-bias  $\theta_u$  of each user  $u$  and 2) generates the debiased rating  $d_{ui}$  of each  
 251 user  $u$  and item  $i$  using the computed bias in the first step. We then theoretically  
 252 show that the debiased ratings generated are unbiased estimators of the true  
 253 preferences of the user for the items rated by them. Thus, the debiased dataset  
 254 can then be fed into various recommender algorithms to generate an unbiased  
 255 predicted rating of a user  $u$  for the item  $i$ , denoted by  $\tilde{d}_{ui}$ . This debiasing  
 256 step ensures that the existing biases are not boosted further in the system.  
 257 Our debiasing model is independent of any recommendation algorithm. We  
 258 show the performance of our debiasing model on both K-nearest neighbors-  
 259 based algorithms (UserKNN, ItemKNN) as well as matrix factorization-based  
 260 algorithms (Alternating Least Square and Singular Value Decomposition) to  
 261 produce the recommendations.

262 In the next step, we use preference corrector to reintroduce the preferences  
 263 of a particular user  $u$  to his/her own recommendations. This is achieved  
 264 via producing a user specific rating  $\tilde{r}_{ui}$  from the debiased rating  $\tilde{d}_{ui}$ . The  
 265 recommendations are re-ranked according to the adjusted ratings, and the  
 266 recommendations are presented to the user. This step ensures that the system  
 267 does not lose accuracy for not considering the preferences of the users. Figure  
 268 1 shows the schematic diagram of our model. Consider that the ratings  $r_{ui}$   
 269 are continuous values ranging from 1 to  $R$ , then mathematically, a biased  
 270 recommender system can be represented as follows:

- 271 1. Each user  $u$ , while rating an item  $i$ , scales down the maximum rating  $R$  by  
 272  $e^{p_{ui}}$ .  $p_{ui}$  is a random variable, drawn from a distribution function  $P_u(I)$ ,  
 273 which has a mean value of  $\alpha_u$ .  $p_{ui}$  represents the logarithm of the true  
 274 preference of the user  $u$  for the item  $i$ . For the sake of brevity, we call it

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log-preference of the user  $u$  for the item  $i$ . Hence  $e^{p_{ui}}$  is a representation of the true preference of user  $u$  for the item  $i$ .

2. In case the item is associated with the disadvantaged group, the user  $u$  further scales down the rating of the item by a factor  $e^{q_{ui}}$ .  $q_{ui}$  is a random variable, drawn from a distribution function  $Q_u(I)$  having a mean value of  $\beta_u$ .  $q_{ui}$  represents the logarithm of the biasedness of the user  $u$  shown to the item  $i$ . For the sake of brevity, we call it the log-bias of the user  $u$  for the book  $i$ . Hence  $e^{q_{ui}}$  represents the biasedness of the user  $u$  for the book  $i$ .
3. For each user  $u$ ,  $\beta_u$  is sampled from the a distribution function  $\Omega(x)$  which governs the global log-bias tendency of the users. We denote the mean value of  $\Omega(x)$  by  $\gamma$ .

Thus, ratings  $r_{ui}$  can be expressed as:

$$r_{ui} = \begin{cases} R/e^{p_{ui}}, & \text{if } i \text{ is associated with advantaged group} \\ R/e^{p_{ui}}e^{q_{ui}}, & \text{if } i \text{ is associated with disadvantaged group} \end{cases} \quad (1)$$

We now present a detailed description of each of the step.

### 3.1 Estimating the mean value for log-bias

The geometric mean of the ratings given by a user  $u$  to the items associated with disadvantaged and advantaged groups, denoted by  $r_{ud}$  and  $r_{ua}$  respectively, are given by the following expressions:

$$r_{ud} = \left( \prod_{i \in \mathbb{D} \cap X_u} r_{ui} \right)^{1/|\mathbb{D} \cap X_u|} \quad \text{and} \quad r_{ua} = \left( \prod_{i \in \mathbb{A} \cap X_u} r_{ui} \right)^{1/|\mathbb{A} \cap X_u|}$$

Further, the log bias in the user profile  $p_u$ , is given by  $\theta_u = \ln \left( \frac{r_{ua}}{r_{ud}} \right)$ .

We use geometric mean to compute the average rating of a user due to the following reasons: 1) It is less biased towards very high scores as compared to arithmetic mean (Neve and Palomares, 2019) and 2) when cold users are involved, aggregating recommendations using the geometric mean is more robust as compared to arithmetic mean (Valcarce et al, 2020).

The below lemma shows that  $\theta_u$  is an unbiased estimator of  $\beta_u$ .

**Lemma 1** *The expectation of log-bias,  $\theta_u$  in the user profile  $p_u$  represents the mean value of the log-bias,  $\beta_u$  of the user  $u$ .*

*Proof* Let us denote  $m = |\mathbb{D} \cap X_u|$  and  $n = |\mathbb{A} \cap X_u|$  to be the number of items associated with disadvantaged and advantaged group respectively in user profile  $p_u$ .



323 Then,

$$\begin{aligned}
 324 \quad \theta_u &= \ln \left( \frac{r_{ua}}{r_{ud}} \right) = \ln \left[ \frac{\left( \prod_{y=1}^m e^{p_{uy}} e^{q_{uy}} \right)^{\frac{1}{m}}}{\left( \prod_{x=1}^n e^{p_{ux}} \right)^{\frac{1}{n}}} \right] && \text{(Using equation 1)} \\
 325 & \\
 326 & \\
 327 & \\
 328 \quad &= \frac{1}{m} \sum_{y=1}^m q_{uy} + \frac{1}{m} \sum_{y=1}^m p_{uy} - \frac{1}{n} \sum_{x=1}^n p_{ux} \\
 329 & \\
 330 &
 \end{aligned}$$

331 Taking expectation both sides:

$$\begin{aligned}
 332 \quad \mathbb{E}[\theta_u] &= \mathbb{E} \left[ \frac{1}{m} \sum_{y=1}^m q_{uy} + \frac{1}{m} \sum_{y=1}^m p_{uy} - \frac{1}{n} \sum_{x=1}^n p_{ux} \right] && (2) \\
 333 & \\
 334 &
 \end{aligned}$$

335 Using linearity of expectation and some simplification, we get:

$$\begin{aligned}
 336 \quad \mathbb{E}[\theta_u] &= \frac{1}{m} \sum_{y=1}^m \mathbb{E}[q_{uy}] + \frac{1}{m} \sum_{y=1}^m \mathbb{E}[p_{uy}] - \frac{1}{n} \sum_{x=1}^n \mathbb{E}[p_{ux}] \\
 337 & \\
 338 & \\
 339 &= \frac{1}{m} \sum_{y=1}^m \beta_u + \frac{1}{m} \sum_{y=1}^m \alpha_u - \frac{1}{n} \sum_{x=1}^n \alpha_u \\
 340 & \\
 341 &
 \end{aligned}$$

342 Thus,  $\mathbb{E}[\theta_u] = \beta_u$ . □

343 Once we get the log biasedness tendencies of users, we use them to produce  
 344 the debiased ratings for the given dataset.

### 346 3.2 Debiasing the Dataset

348 The debiased rating of the item  $i$  associated with disadvantaged group and  
 349 rated by user  $u$  is given as  $d_{ui} = r_{ui}e^{\theta_u}$ . We now provide the main theorem of  
 350 our paper.

352 **Theorem 2**  $\ln(d_{ui})$  is the unbiased estimator of the log of the true rating of the item  
 353  $i$ .

356 *Proof*  $\ln(d_{ui}) = \theta_u + \ln(r_{ui}) = \theta_u + \ln R - p_{ui} - q_{ui}$ . Last equality is obtained from  
 357 Equation 1. Taking expectation both sides:

$$\begin{aligned}
 358 \quad \mathbb{E}(\ln(d_{ui})) &= \mathbb{E}[\theta_u] + \mathbb{E}[\ln R] - \mathbb{E}[q_{ui}] - \mathbb{E}[p_{ui}] \\
 359 &= \beta_u + \ln R - \beta_u - \alpha_u && \text{(Using Lemma 1)} \\
 360 & \\
 361 &= \ln R - \alpha_u = \ln \left( \frac{R}{e^{\alpha_u}} \right) \\
 362 &
 \end{aligned}$$

363 As we can see, the expected value of  $\ln(d_{ui})$  contains only the term representing  
 364 the true preference of the item for user  $u$ . □

366 Thus, instead of  $r_{ui}$ , ratings  $d_{ui}$  are fed into the recommender system to  
 367 generate the predicted unbiased ratings  $\tilde{d}_{ui}$ . Simply removing the bias from  
 368 the user's rating could severely affect the system's accuracy because the bias

of an individual user reflects their taste. However, the debiasing step helps prevent the bias of one user from affecting the recommendation of other users. Next, we use preference corrections by correcting the predicted rating of the user with respect to his/her own preference parameter.

### 3.3 Preference Correction to Improve Accuracy

Note that when the users are inherently biased against a group of items,  $\mathcal{D}$  then showing the items from  $\mathcal{D}$  naively to these users will severely affect the accuracy of the system. The goal of this work is not just to promote the exposure of the items among the two groups but is to not let the bias of one user creep into the bias of the other user. This was achieved via debiasing the dataset. Once the debiased ratings are generated, the accuracy of the system is maintained by introducing a correction factor. Although providing us with higher accuracy, the idea to re-introduce the correction factor may lead to an overall increase in the individual biases. This on a prima-facie may look self-defeating, but we need to note that final ratings still have significantly less bias than original ratings. If we do not introduce the correction factor, the users might flock to a substantial bias platform due to poor accuracy.

The correction is achieved via multiplying the predicted ratings of items associated with disadvantaged group by a factor  $e^{-\theta_u}$ . Thus, the final recommended ratings will be given as  $\tilde{r}_{ui} = \tilde{d}_{ui}e^{-\theta_u}$ . Similar to the calculation of bias in the dataset, we can now compute the bias in the recommendation profile.

### 3.4 Bias in recommendation profile

We generate recommendations for the users in the test set  $\mathcal{T}$ . The recommendation profile for a user  $u \in \mathcal{T}$  is denoted by  $\tilde{p}_u = \{\tilde{X}_u, \tilde{R}_u\}$ , which represents the set of recommended books ( $\tilde{X}_u$ ) for the user  $u$  and their predicted ratings ( $\tilde{R}_u = \{\tilde{r}_{ui}\}_{i \in \tilde{X}_u}$ ). Let the set of items associated with disadvantaged and advantaged groups be denoted by  $\tilde{\mathbb{D}}$  and  $\tilde{\mathbb{A}}$  respectively. The average predicted ratings of the items associated with disadvantaged and advantaged groups, denoted by  $\tilde{r}_{ud}$  and  $\tilde{r}_{ua}$  respectively, are given by:  $\tilde{r}_{ud} = (\prod_{i \in \tilde{\mathbb{D}} \cap \tilde{X}_u} \tilde{r}_{ui})^{1/|\tilde{\mathbb{D}} \cap \tilde{X}_u|}$  and  $\tilde{r}_{ua} = (\prod_{i \in \tilde{\mathbb{A}} \cap \tilde{X}_u} \tilde{r}_{ui})^{1/|\tilde{\mathbb{A}} \cap \tilde{X}_u|}$  where  $\tilde{r}_{ui}$  is the predicted rating given to item  $i$  in the recommendation-profile generated for a user  $u$ . The log-bias in the recommendation-profile  $p_u$ , denoted by  $\tilde{\theta}_u$ , is then given by  $\tilde{\theta}_u = \ln \left( \frac{\tilde{r}_{ua}}{\tilde{r}_{ud}} \right)$ . For an unbiased recommendation-profile,  $\tilde{\theta}_u = 0$ . A profile biased against disadvantaged groups will have  $\tilde{\theta}_u > 0$ . We can then compute the overall bias of the recommender system by taking the average overall users, and this average gives us the estimated value of  $\gamma$ .

## 4 Dataset

To evaluate the proposed model, we run experiments on two publicly available book rating datasets, the Book-Crossing dataset, originally put together by

Statistic	Amazon	Book-Crossing
Number of male authored books	58369	829
Number of female authored books	58220	806
Number of users	44792	376

**Table 1:** Dataset details

Ziegler et al (2005b) and the Amazon Book Review dataset, put together by Ni et al (2019). We further process this dataset through the following stages:

#### 4.1 Book Author Identification

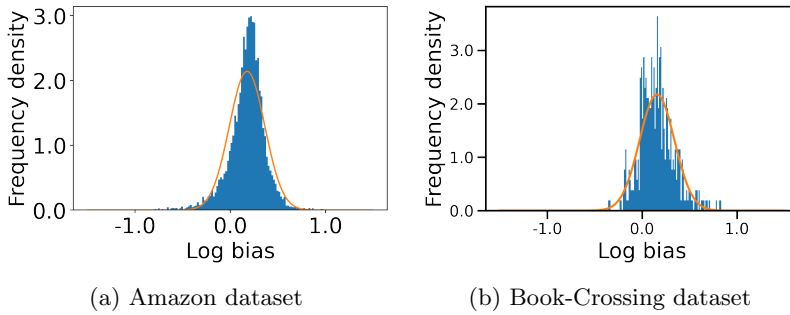
Their unique ISBNs identify the books in both datasets. We identified the authors of the books present in the datasets via their ISBN numbers using the following three API services: *Google Books API APIs* (Accessed: 2021-02-24), *ISBNdb API ISBNDB* (Accessed: 2021-02-27), and *Open Library API OpenLibrary* (Accessed: 2021-03-02). We could not identify the authors of some of the books. Hence we discarded those books from the dataset.

#### 4.2 Author Gender Identification

We identified the genders of the authors via their first names. We used *Genderize.io the gender of a name* (Accessed: 2021-03-5), an API service dedicated to identifying the gender given the first name of the person. We used a minimum confidence threshold of 90% for gender identification. We could not identify the gender of some of the authors. We discard the books written by those authors from the dataset.

#### 4.3 Filtering

We filtered the Book-Crossing dataset to include only those books with at least 50 ratings and only those users who have rated at least 50 books. Amazon dataset was significantly larger as compared to the Book-Crossing dataset. We filtered it to include only those books with at least 100 ratings and only those users who have rated at least 100 books. We did this filtering so that recommender algorithms have much data to produce accurate recommendations. The statistics of filtered datasets are mentioned in Table 1. The number of books written by male authors is almost equal to that of female authors for both datasets.



**Fig. 2:** User log-bias in the original dataset

## 5 Experimental Results

### 5.1 Input Bias

We show the distributions of log-bias tendency ( $\theta_u$ ) of the users in the Amazon dataset and the Book-Crossing dataset in Figure 2. We observe that the mean log-bias tendency over all the users in the Amazon dataset is higher (0.176) than that of the Book-Crossing dataset (0.157)<sup>1</sup>.

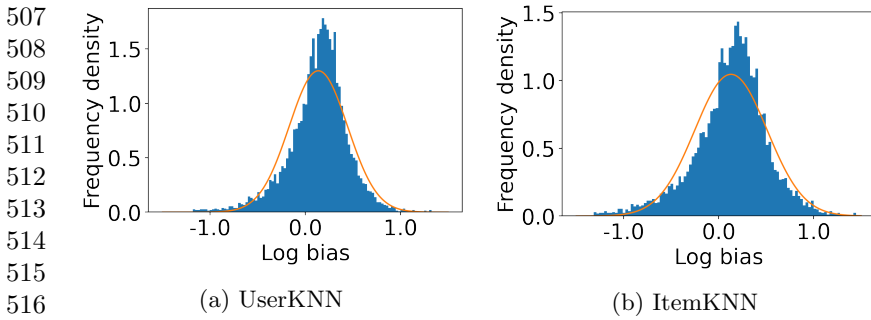
### 5.2 Output Bias

We randomly separate 20% of users in each dataset as the test group. We generate the recommendations for the users in the test group using two K-nearest neighbors-based algorithms, UserKNN and ItemKNN, and two matrix factorization-based algorithms, Alternating Least Square and Singular Value Decomposition. These algorithms were selected because the accuracy and ranking relevancy of the recommendations produced by them were among the highest values compared with other algorithms. Hence coupling our model with them would best highlight the effects brought about by the same. We calculate the estimated value of log-bias ( $\hat{\theta}_u$ ) and accuracy in the recommendations separately for each algorithm applied on the two datasets. For this, we use two error measures, the Root Mean Squared Error (RMSE) and the Mean Absolute Error (MAE), and two ranking relevance parameters, Normalized Discounted Cumulative Gains and Mean Reciprocal Rank.

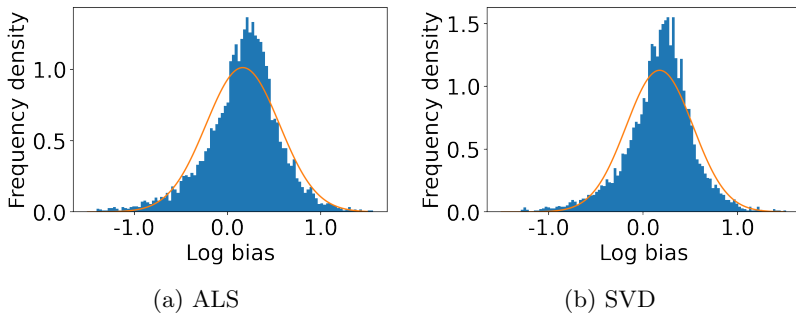
We first begin plotting the log-bias ( $\hat{\theta}_u$ ) distribution for the recommendations produced by the algorithms without employing our debiased model in Figures 3 and 4 for Amazon datasets with respect to K-nearest neighbor family and matrix factorization family of algorithms. Figures 5 and 6 similarly present the log-bias distribution for the recommendations produced by the two family of algorithms for Book-Crossing datasets respectively without employing our debiased model. We compute the log-bias by feeding biased ratings  $r_{ui}$  to the

<sup>1</sup>code is available at <https://github.com/venomNomNom/genderBias.git>

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**Fig. 3:** Output log-bias in AZ dataset without employing the model under K-nearest neighbour family of algorithms

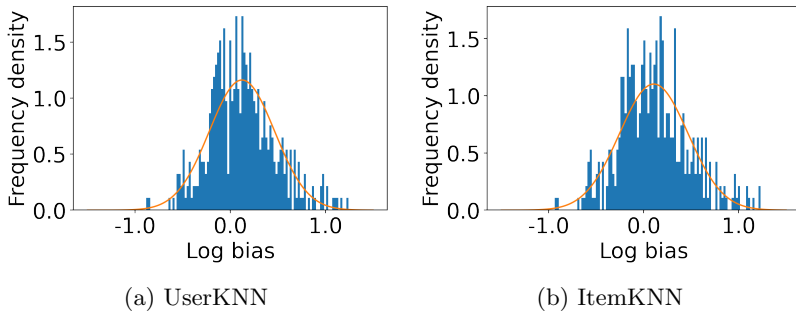


**Fig. 4:** Output log-bias in AZ dataset without employing the model under matrix factorization family of algorithms

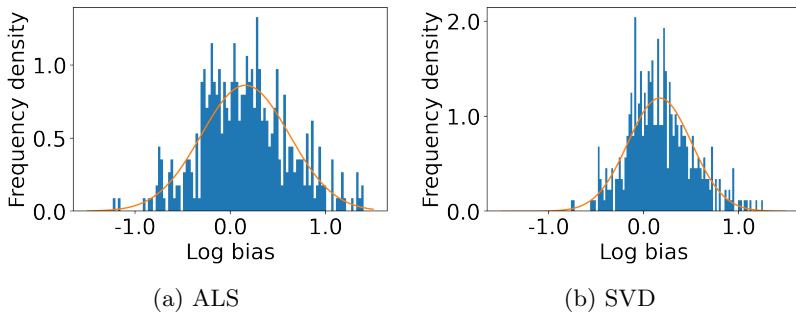
four algorithms. As can be seen from the figures, that the output log biasedness was very similar to what was observed in the input data.

We next deploy our model partially. We leave out the preference correction phase and produce the recommendations using the algorithms mentioned before by feeding the debiased ratings  $d_{ui}$  to these algorithms. We estimate the mean log-bias tendency in the recommendations  $\tilde{\theta}_u$  using debiased ratings produced by the algorithms  $\tilde{d}_{ui}$ . The log-bias ( $\tilde{\theta}_u$ ) distribution for the recommendations produced by the algorithms after partial deployment of the model is depicted in the Figures 7 and 8 for Amazon dataset and in the Figures 9 and 10 for book crossing dataset. As can be seen, there is a significant reduction in log-bias tendency (64.38%) in the Amazon dataset and (53.67%) in Book-Crossing dataset for the UserKNN algorithm. However, we also see an increase in error rates on both datasets. This is because the test data itself contains biases.

Finally, we deploy our complete model after adding the preference correction method and repeat the experiment. The log-bias ( $\tilde{\theta}_u$ ) distribution for the recommendations produced by the algorithms after deployment of the complete



**Fig. 5:** Output log-bias in BX dataset without employing the model under K-nearest neighbour family of algorithms



**Fig. 6:** Output log-bias in BX dataset without employing the model under matrix factorization family of algorithms

model is depicted in Figures 11, 12 for Amazon dataset and in Figures 13, 14 for book crossing dataset. The final values for all the cases are given in Table 2 for Amazon dataset and in Table 3 for book crossing datasets. As can be seen, there is still a significant reduction in mean log-bias tendency, which reduces by 42.39% in the Amazon dataset and by 37.82% in the case of the Book-Crossing dataset for UserKNN algorithm. The accuracy loss, however, is insignificant, making this trade-off advantageous. Figure 15 presents the percentage gain in bias reduction for both the dataset. The percentage loss in accuracy is depicted in figures 16 and 17 for Amazon and Book-Crossing datasets respectively. The percentage loss in ranking relevancy metrics are depicted in figures 18 and 19 respectively.

We next conduct significance testing to validate the log-bias reduction. Tables 4 and 5 show the p-values obtained from left-tail significance tests on the log-bias of the recommendations made for the users in the sample. We can see from the p-value for the Amazon datasets that the bias reduction is significant. For the Book-Crossing dataset, the significance of the bias reduction is less pronounced. One of the prominent reasons for this is that the test sample size

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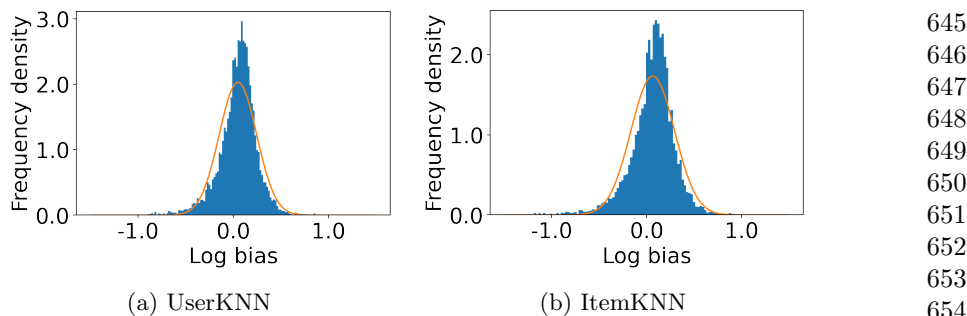
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Case	Algorithm	Mean log-bias	RMSE	MAE	NDCG	Ranking Relevancy
without model	UserKNN	0.137	0.808	0.693	0.452	0.498
	ItemKNN	0.129	0.736	0.580	0.597	0.643
	ALS	0.164	0.873	0.829	0.281	0.447
	SVD	0.175	0.790	0.753	0.342	0.471
without preference correction phase	UserKNN	0.049	1.103	0.921	0.0224	0.0278
	ItemKNN	0.063	1.076	0.873	0.0229	0.0204
	ALS	0.093	1.281	1.1211	0.0161	0.0394
	SVD	0.071	1.257	1.183	0.0138	0.0206
with preference correction phase	UserKNN	0.079	0.871	0.738	0.3982	0.4462
	ItemKNN	0.080	0.824	0.661	0.5236	0.6121
	ALS	0.121	0.982	0.903	0.2391	0.3853
	SVD	0.103	0.872	0.847	0.2989	0.4159

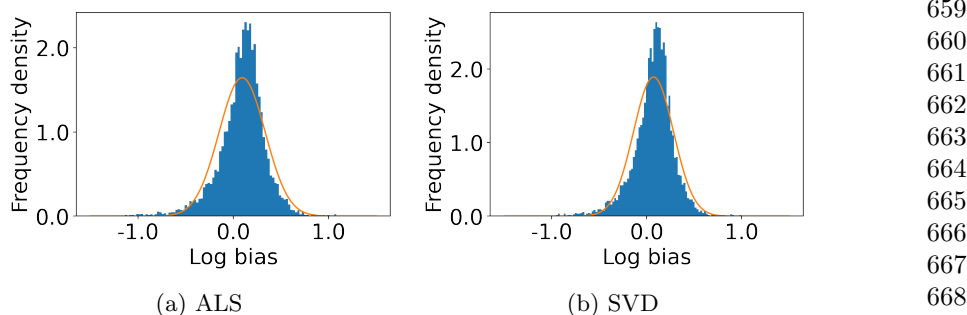
**Table 2:** Summary of Results for Amazon Dataset

Case	Algorithm	Mean log-bias	RMSE	MAE	NDCG	Ranking Relevancy
without model	UserKNN	0.122	1.580	1.178	0.264	0.272
	ItemKNN	0.106	1.511	1.304	0.313	0.412
	ALS	0.158	1.815	1.642	0.235	0.370
	SVD	0.169	1.761	1.626	0.277	0.296
without preference correction phase	UserKNN	0.057	2.468	1.754	0.0232	0.0245
	ItemKNN	0.054	2.463	2.055	0.0142	0.0271
	ALS	0.087	2.752	2.175	0.0421	0.0736
	SVD	0.072	2.601	1.979	0.0261	0.0240
with preference correction phase	UserKNN	0.076	1.799	1.298	0.2099	0.2317
	ItemKNN	0.073	1.785	1.516	0.2538	0.3560
	ALS	0.119	2.022	1.768	0.1626	0.2831
	SVD	0.114	1.988	1.731	0.2258	0.2481

**Table 3:** Summary of Results for Bookcrossing Dataset



**Fig. 7:** Output log-bias in AZ dataset with debiasing under family of K-nearest neighbour algorithms



**Fig. 8:** Output log-bias in AZ dataset with debiasing under family of matrix factorization algorithms

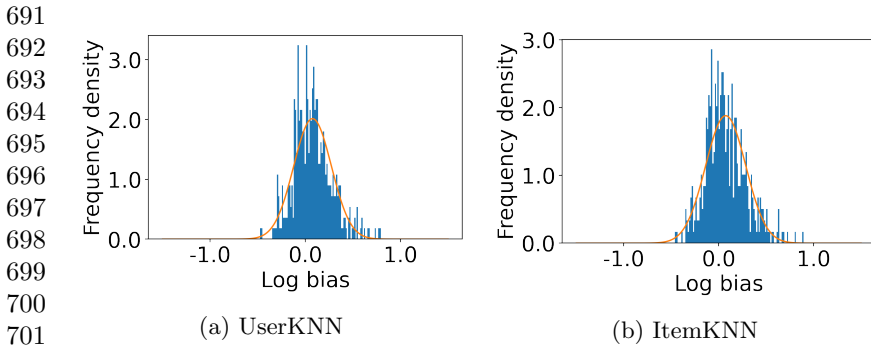
Algorithm	$\bar{x}$	$\mu$	$\sigma$	$z$	$p$
UserKNN	0.079	0.137	0.307	-17.90	$< 10^{-5}$
ItemKNN	0.080	0.129	0.381	-12.06	$< 10^{-5}$
ALS	0.121	0.164	0.394	-10.46	$< 10^{-5}$
SVD	0.103	0.175	0.354	-19.27	$< 10^{-5}$

**Table 4:** Significance test results for bias reduction for Amazon Dataset

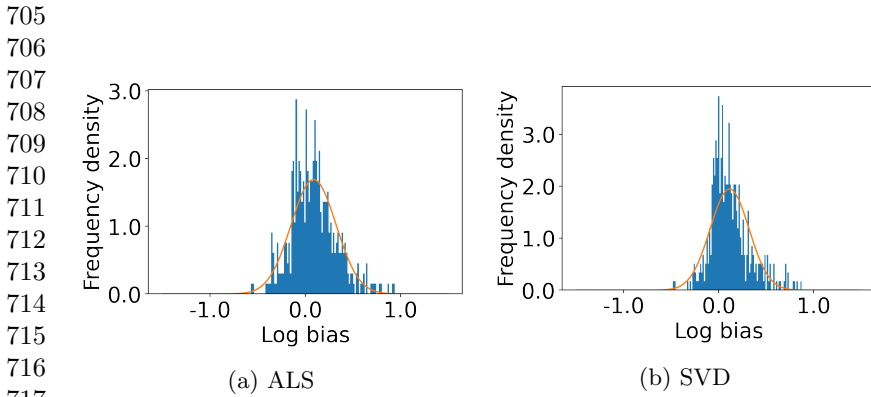
for the Book-Crossing dataset was relatively small due to the small number of users in the dataset. In essence, the utility of the recommender system is maintained while reducing the log-bias tendency in the recommendations.

We further observe that the bias reduction is more in the case of UserKNN based recommendations than the ItemKNN based recommendations. This observation can be attributed to the fact that our model addresses the bias originating from the distortion in ratings from the users' side. It compares the ratings of an item given by a particular user with the appropriately scaled average of ratings given by other users to that item in the dataset. It, therefore,

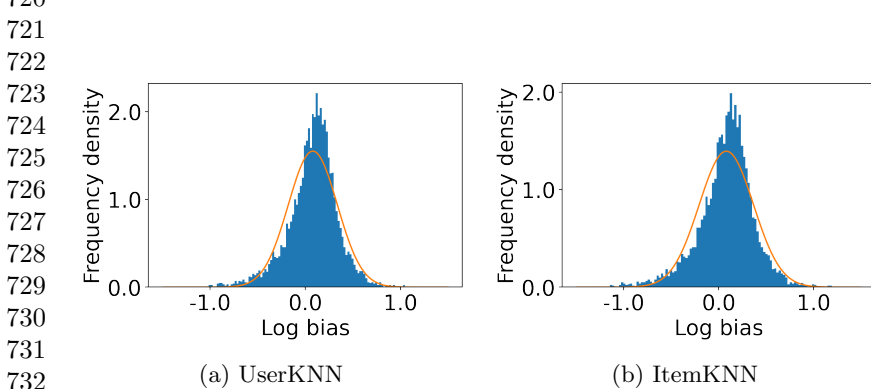




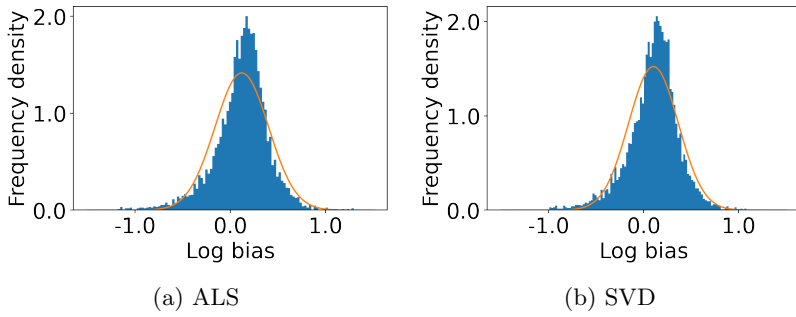
702 **Fig. 9:** Output log-bias in BX dataset with debiasing under family of K-nearest  
703 neighbour algorithms  
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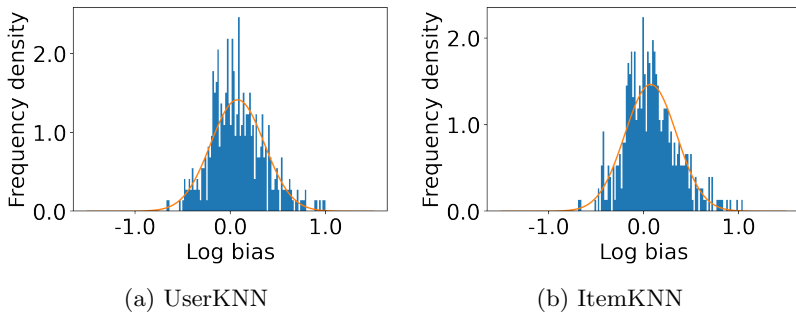
718 **Fig. 10:** Output log-bias in BX dataset with debiasing under family of matrix  
719 factorization algorithms  
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733 **Fig. 11:** Output log-bias in AZ dataset with Preference correction under family  
734 of K-nearest neighbour algorithms  
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**Fig. 12:** Output log-bias in AZ dataset with Preference correction under family of matrix factorization algorithms

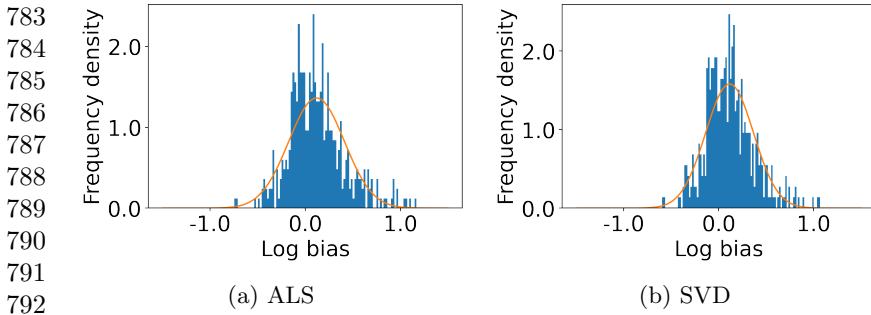


**Fig. 13:** Output log-bias in BX dataset with reinserting the biases under family of K-nearest neighbour algorithms

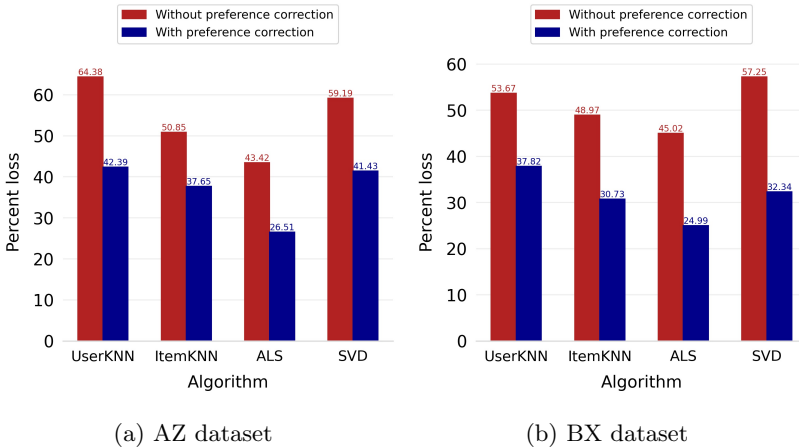
Algorithm	$\bar{x}$	$\mu$	$\sigma$	$z$	$p$
UserKNN	0.076	0.122	0.343	-1.164	0.122
ItemKNN	0.073	0.106	0.362	-0.780	0.218
ALS	0.119	0.158	0.464	-0.738	0.230
SVD	0.114	0.169	0.335	-1.413	0.079

**Table 5:** Significance test results for bias reduction for Bookcrossing Dataset

resonates with the UserKNN algorithm, which predicts the ratings of an item for a particular user based on the ratings of that item for his or her peers. The ItemKNN algorithm, on the other hand, predicts the ratings of an item for a particular user based on the ratings given to similar items by that user. The model does not sit squarely with ItemKNN. Thus the bias reduction in UserKNN is more as compared to that in the case of ItemKNN. We further observe that the bias reduction is more in the case of the AZ dataset as compared to the BX dataset. This observation can be attributed to the AZ dataset having a higher input mean log-bias tendency. Further, the AZ dataset has a significantly larger



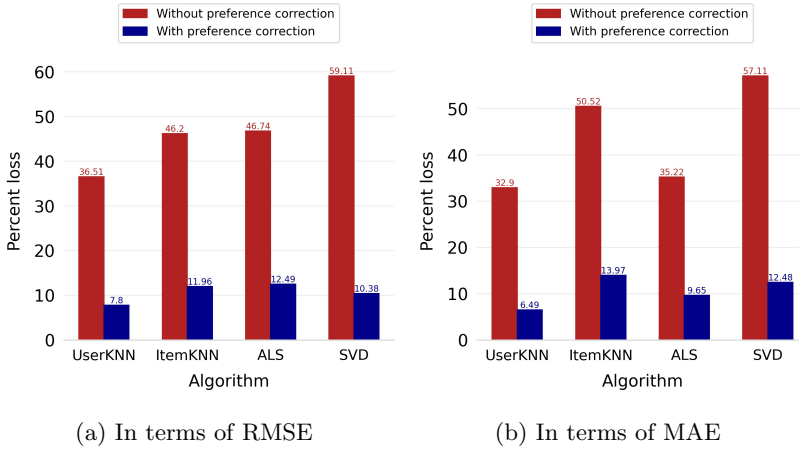
**Fig. 14:** Output log-bias in BX dataset with reinserting the biases under family of matrix factorization algorithms



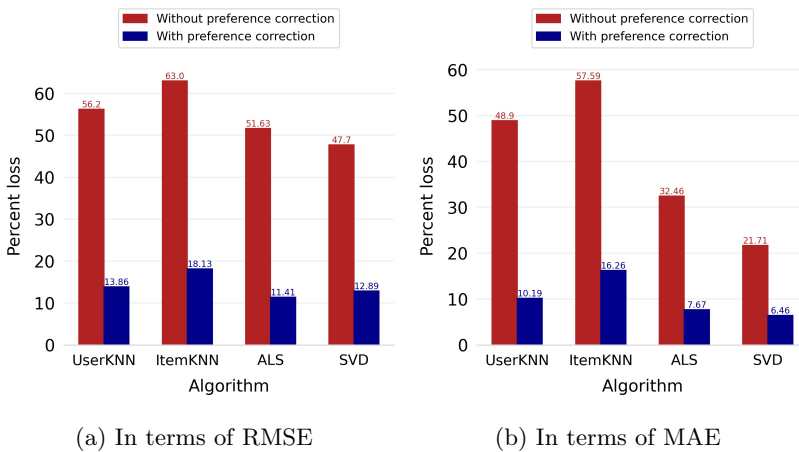
**Fig. 15:** Bias reduction

number of users and items which leads to a more accurate estimation of user bias scores and, therefore, more effective bias mitigation.

We observe that accuracy and ranking relevancy loss is, in general, higher for ItemKNN as compared to UserKNN. This is due to the fact that the model quantifies the bias of users by comparing the ratings given by them to particular items with a scaled average of ratings given by their peers to those items. This resonates with the UserKNN algorithm, which predicts user ratings for particular items based on the ratings of similar users. Thus the model is better oriented towards the UserKNN algorithm, giving better accuracy and bias reduction in its case. In the case of matrix factorization algorithms, the accuracy and ranking relevancy losses are relatively comparable. It is not clear which one of the two algorithms is more coherent with the model.



**Fig. 16:** Accuracy loss for AZ dataset



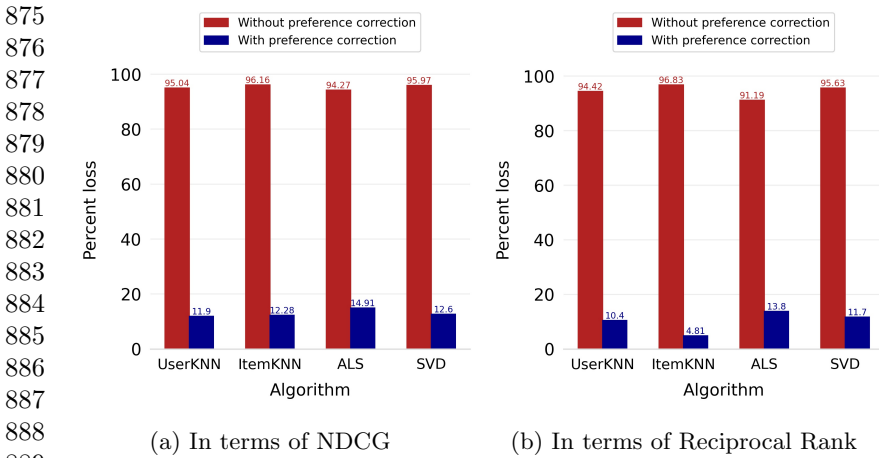
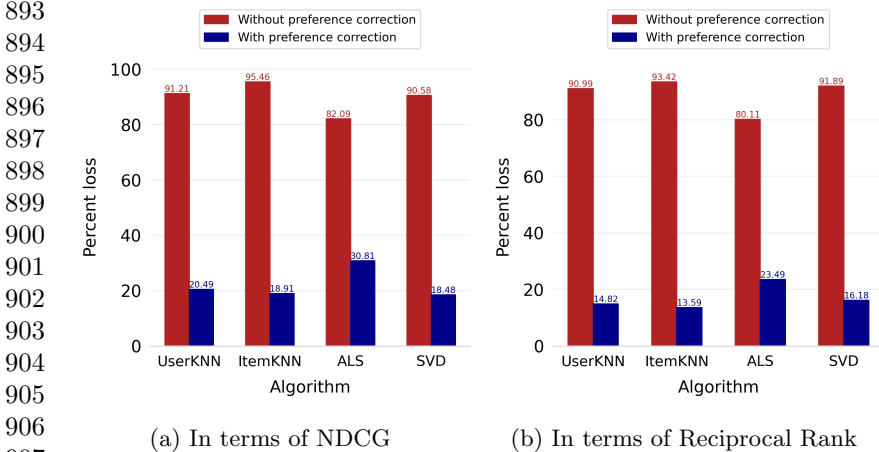
**Fig. 17:** Accuracy loss for BX dataset

We further observe that accuracy loss on BX dataset is higher than that of AZ dataset. This observation can be attributed to the fact that the user and item base of the AZ dataset is higher as compared to the BX dataset. Thus, the bias score estimates are more accurate, which provides more accurate predictions of the item scores for the users when reinserted into the recommendations.

## 6 Conclusion and Future Work

We proposed a model to quantify and mitigate the bias in the explicit feedback given by the users to different items. We theoretically showed that the debiased

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**Fig. 18:** Ranking relevancy loss for AZ dataset**Fig. 19:** Ranking relevancy loss for BX dataset

911 ratings produced by our model are unbiased estimators of the true preference  
 912 of the users for the books. With the help of comprehensive experiments on  
 913 two publically available book datasets, we show a significant reduction in the  
 914 bias (almost 40%) with just 10% decrease in accuracy using the UserKNN  
 915 algorithm. Similar trends were observed for other algorithms such as ItemKNN,  
 916 ALS, and SVD. Our model is independent of these algorithms' choices and can  
 917 be applied with any recommendation algorithm. We used book recommender  
 918 system because we were able to generate the gender information from publicly  
 919 available APIs. Our model is not restricted to book recommender system as long  
 920 as protected attribute information about the items is known. We leave extension

of the model to missing protected attribute as an interesting future work. It will 921  
 be an interesting direction to see if the ideas from fair classification literature 922  
 with missing protected attributes (Coston et al, 2019) can be leveraged. We 923  
 further did not address the bias originating from fewer ratings for a female- 924  
 authored book than a male-authored one. We leave extending the model to 925  
 the bias originating from lesser number of ratings and extensively studying the 926  
 model for other recommender systems as the future directions. 927

## Declaration 928

### Ethical Approval and Consent to participate 929

All authors certify that they have no affiliations with or involvement in any 930  
 organization or entity with any financial interest or non-financial interest in the 931  
 subject matter or materials discussed in this manuscript. 932  
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### Consent for publication 934

Authors give full consent for publications 935  
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### Human and Animal Ethics 937

Not Applicable 938  
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### Availability of supporting data 940

Dataset is publicly available and code is already made available on github. 941  
 942

### Competing interests 943

The authors declare that they have no conflict of interest. 944  
 945

### Funding 946

The project is supported by Science and Engineering Research Board, India 947  
 with project number SRG/2020/001138. 948

### Authors' contributions 949

Shrikant Saxena is the main contributing author of the paper. Shweta Jain has 950  
 helped in writing the manuscript. All authors have reviewed the paper. 951  
 952

### Acknowledgments 953

Not applicable. 954  
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